

# APPLIED FINANCE

## Lecture 12

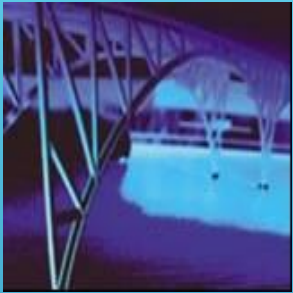




# SOLVING THE FV PROBLEM

Inputs	5	10	-10,000	0	
	N	I/Y	PV	PMT	FV
Compute					16,105.10

The result indicates that a **\$10,000** investment that earns **10%** annually for **5 years** will result in a future value of **\$16,105.10**.



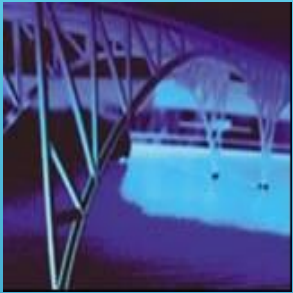
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Quick! How long does it take to double \$5,000 at a compound rate of 12% per year (approx.)?

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We will use the “Rule-of-72”.

**DOUBLE YOUR MONEY!!!**



Quick! How long does it take to double \$5,000 at a compound rate of 12% per year (approx.)?

*Approx. Years to Double =  $72 / i\%$*

## THE “RULE-OF-72”

$$72 / 12\% = \underline{6 \text{ Years}}$$

[Actual Time is 6.12 Years]

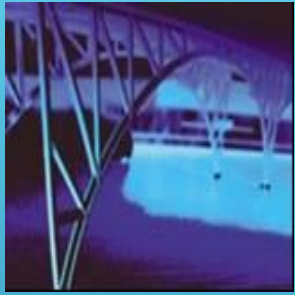


# SOLVING THE PERIOD PROBLEM

Inputs	12	-1,000	0	+2,000	
	N	I/Y	PV	PMT	FV
Compute	6.12 years				

The result indicates that a **\$1,000** investment that earns **12%** annually will double to **\$2,000** in **6.12 years**.

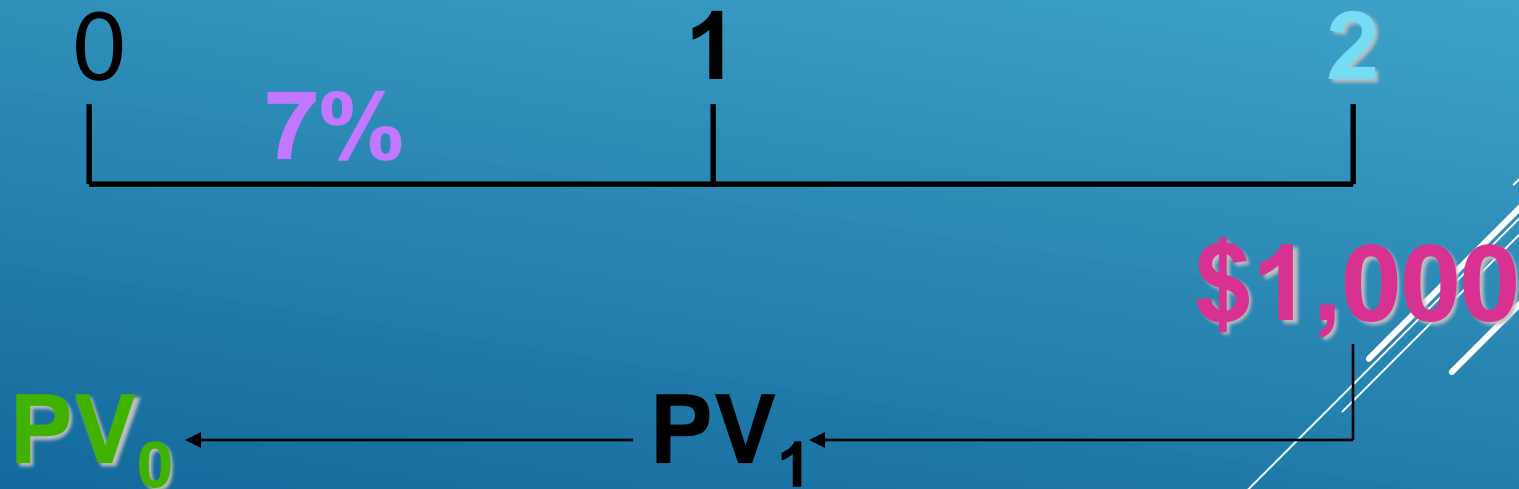
*Note:  $72/12\% = \text{approx. } 6 \text{ years}$*



# PRESENT VALUE DEPOSIT (GRAPHIC)

## SINGLE

Assume that you need **\$1,000** in 2 years.  
Let's examine the process to determine how much you need to deposit today at a discount rate of **7%** compounded annually.

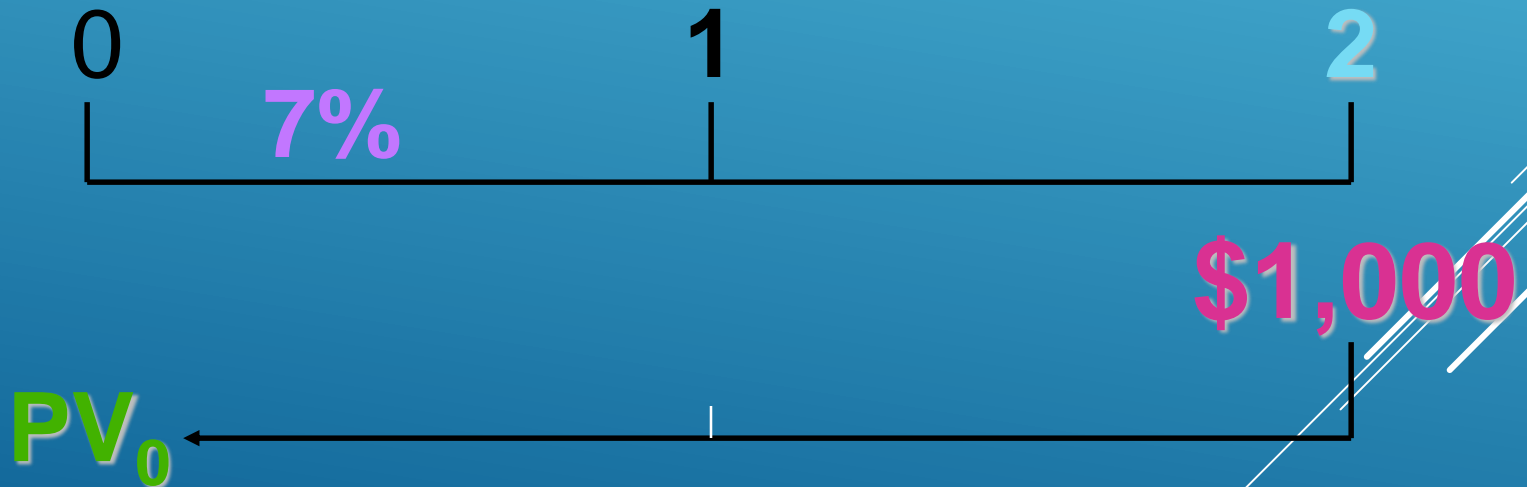




# PRESENT VALUE SINGLE DEPOSIT (FORMULA)

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$$PV_0 = FV_2 / (1+i)^2 = \$1,000 / (1.07)^2 = FV_2 / (1+i)^2 = \$873.44$$





# GENERAL PRESENT VALUE FORMULA

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$$PV_0 = FV_1 / (1+i)^1$$

$$PV_0 = FV_2 / (1+i)^2 \text{ etc.}$$

General Present Value Formula:

$$PV_0 = FV_n / (1+i)^n$$

or  $PV_0 = FV_n (PVIF_{i,n})$  -- See Table II



## VALUATION USING TABLE II

**PVIF<sub>i,n</sub>** is found on Table II

at the end of the book.

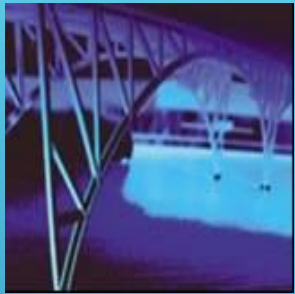
Period	6%	7%	8%
1	.943	.935	.926
2	.890	.873	.857
3	.840	.816	.794
4	.792	.763	.735
5	.747	.713	.681

# USING PRESENT VALUE TABLES

$$PV_2 = \$1,000 (PVIF_{7\%,2})$$

$$\text{Period} = \$1,000 (.873) \quad 6\% \quad 7\% \quad 8\%$$

Period	6%	7%	8%
1	.943	.935	.916
2	.890	.873	.857
3	.840	.816	.794
4	.792	.763	.735
5	.747	.713	.681





# SOLVING THE PV PROBLEM

<b>Inputs</b>	2	7		0	+1,000
	<b>N</b>	<b>I/Y</b>	<b>PV</b>	<b>PMT</b>	<b>FV</b>
<b>Compute</b>			<b>-873.44</b>		

**N:** 2 Periods (enter as 2)

**I/Y:** 7% interest rate per period (enter as 7 NOT .07)

**PV:** Compute (Resulting answer is negative “deposit”)

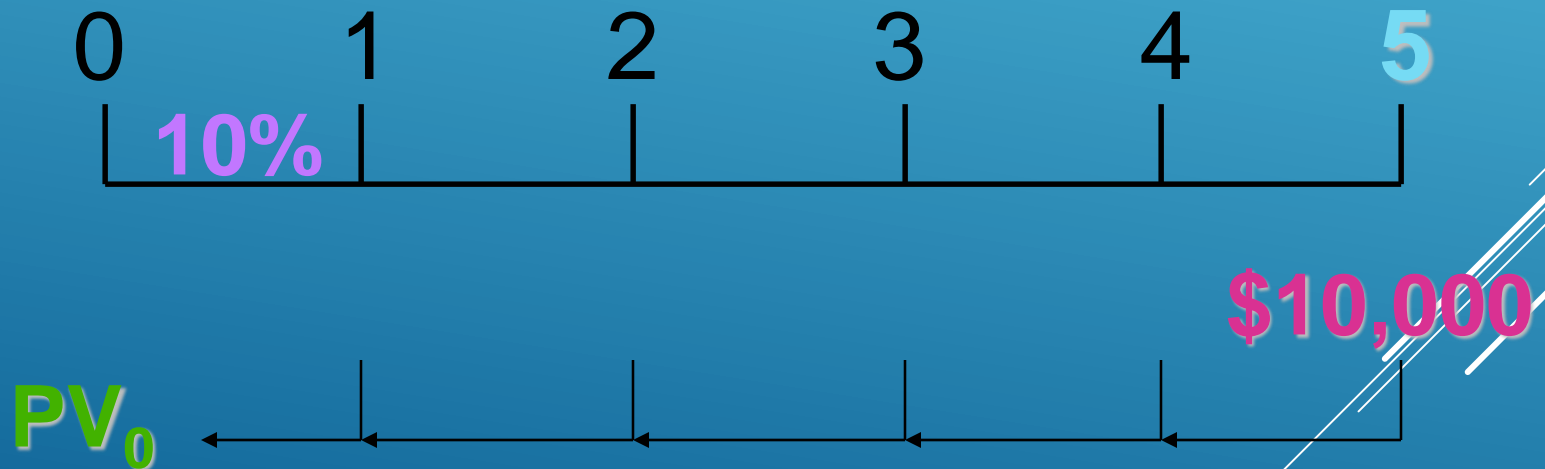
**PMT:** Not relevant in this situation (enter as 0)

**FV:** \$1,000 (enter as positive as you “receive \$”)



## STORY PROBLEM EXAMPLE

Julie Miller wants to know how large of a deposit to make so that the money will grow to **\$10,000** in **5 years** at a discount rate of **10%**.





# STORY PROBLEM SOLUTION

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- ▶ Calculation based on general formula:

$$PV_0 = FV_n / (1+i)^n$$
$$\$10,000 / (1 + 0.10)^5 = \$6,209.21$$

- ▶ Calculation based on Table I:

$$= \$10,000 (PVIF_{10\%, 5}) = \$10,000$$
$$(.621) = \$6,210.00$$

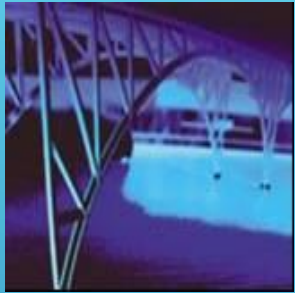
*[Due to Rounding]*



# SOLVING THE PV PROBLEM

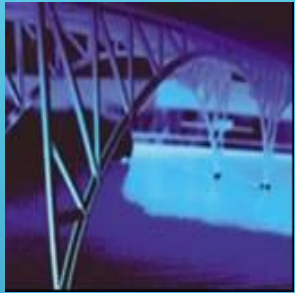
Inputs	5	10		0	+10,000
	N	I/Y	PV	PMT	FV
Compute			-6,209.21		

The result indicates that a \$10,000 future value that will earn 10% annually for 5 years requires a \$6,209.21 deposit today (present value).



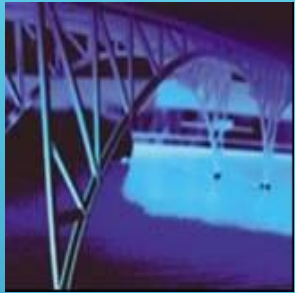
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- ◆ ***An Annuity*** represents a series of equal payments (or receipts) occurring over a specified number of equidistant periods.
  - ▶ Ordinary Annuity: Payments or receipts occur at the end of each period.
  - ▶ Annuity Due: Payments or receipts occur at the beginning of each period.

## TYPES OF ANNUITIES

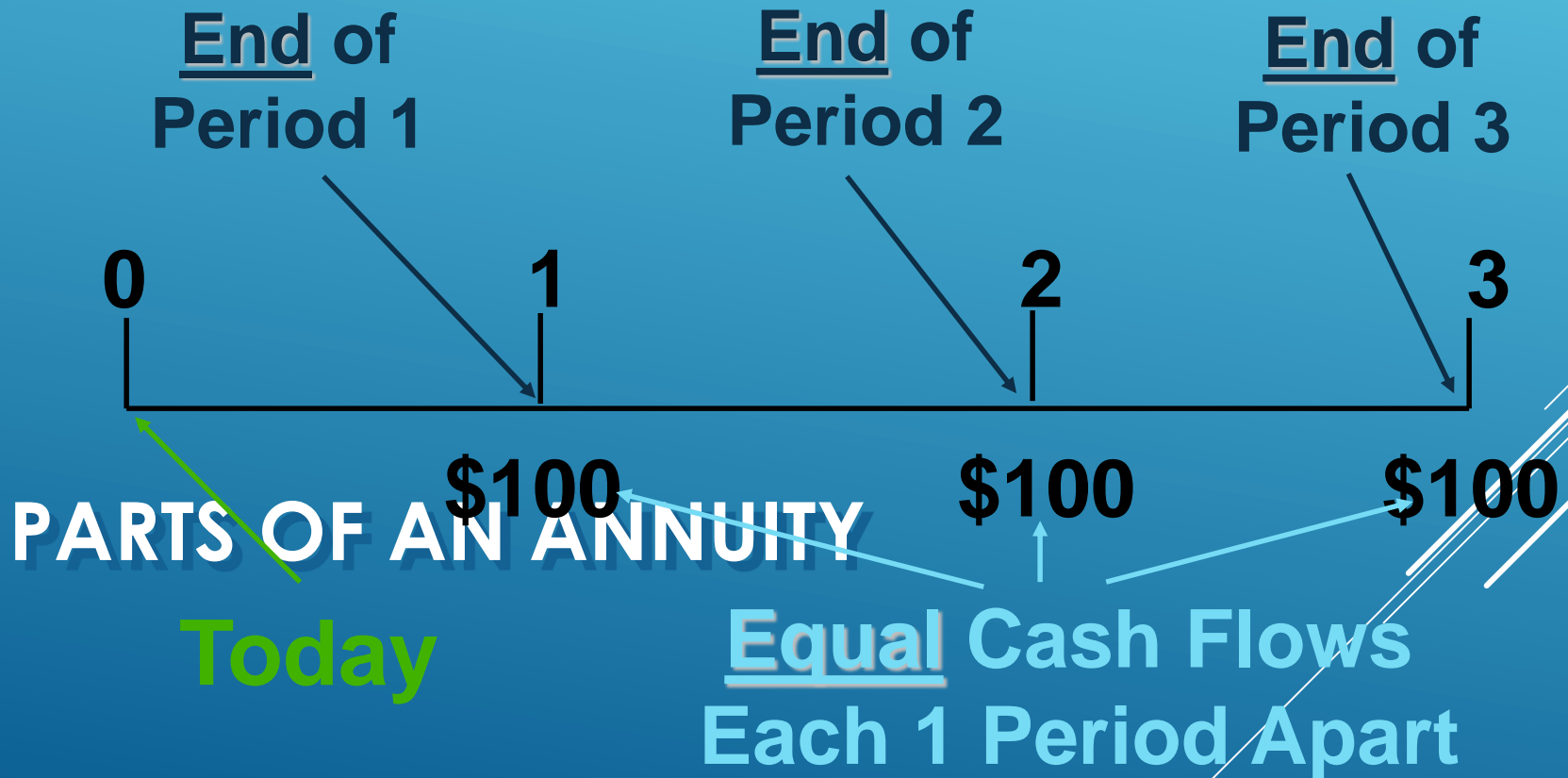


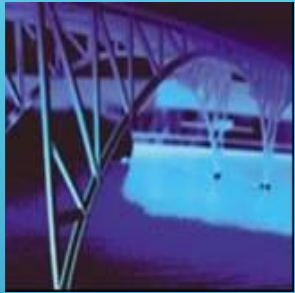
- ▶ Student Loan Payments
- ▶ Car Loan Payments
- ▶ Insurance Premiums
- ▶ Mortgage Payments
- ▶ Retirement Savings

## EXAMPLES OF ANNUITIES



(Ordinary Annuity)





(Annuity Due)

Beginning of  
Period 1

Beginning of  
Period 2

Beginning of  
Period 3

0

1

2

3

\$100

\$100

\$100

PARTS OF AN ANNUITY

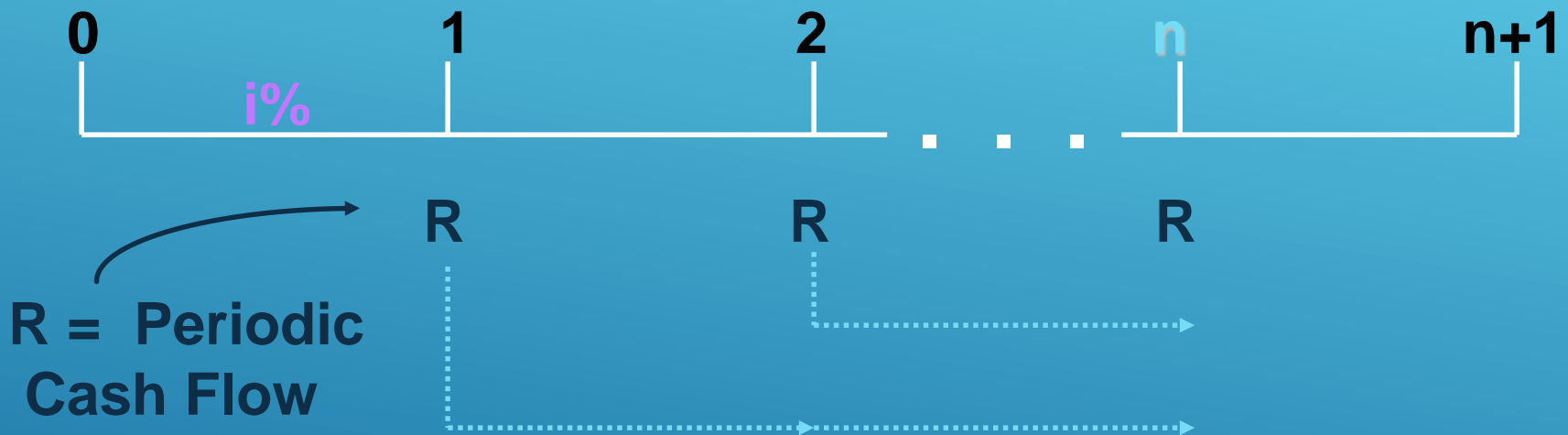
Today

Equal Cash Flows  
Each 1 Period Apart



# OVERVIEW OF AN ORDINARY ANNUITY -- FVA

Cash flows occur at the end of the period



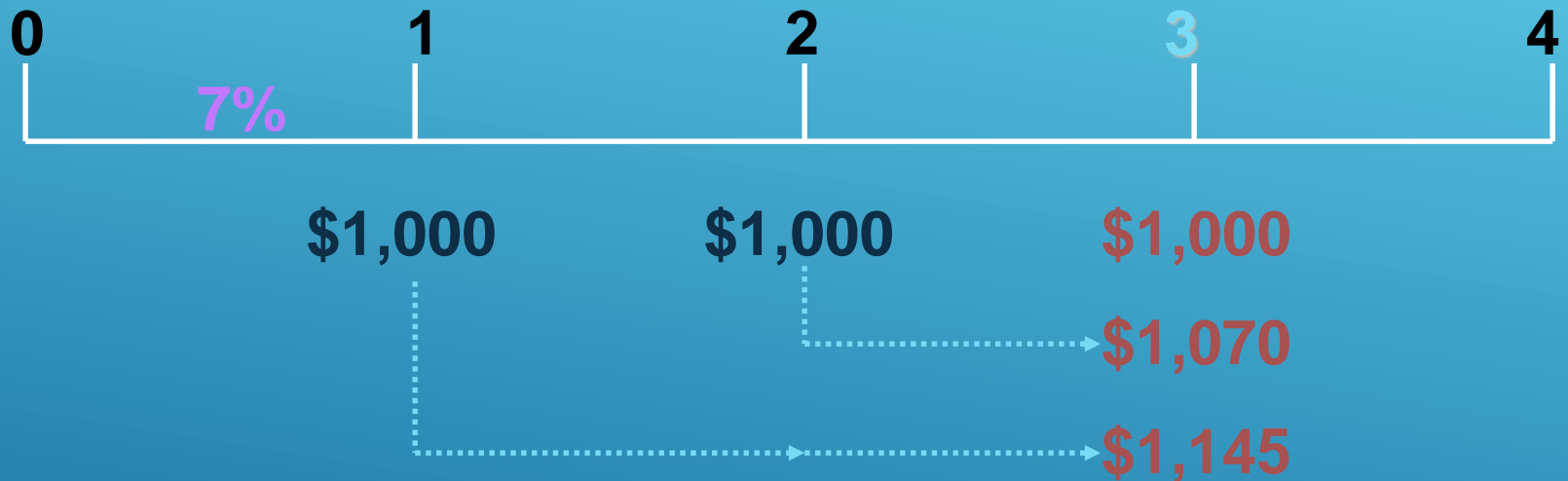
$$FVA_n = R(1+i)^{n-1} + R(1+i)^{n-2} + \dots + R(1+i)^1 + R(1+i)^0$$

$FVA_n$



# EXAMPLE OF AN ORDINARY ANNUITY -- FVA

Cash flows occur at the end of the period



$$\begin{aligned} FVA_3 &= \$1,000(1.07)^2 + \\ & \$1,000(1.07)^1 + \$1,000(1.07)^0 \\ &= \$1,145 + \$1,070 + \$1,000 \\ &= \$3,215 \end{aligned}$$

$$\underline{\$3,215 = FVA_3}$$