

Bitcoin and Cryptocurrencies

- Lecture 1: Bitcoin networks
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Online Transactions

- Physical cash
 - Non-traceable (well, mostly!)
 - Secure (mostly)
 - Low inflation
- Can't be used online directly
- Electronic credit or debit transactions
 - ◆ Bank sees all transactions
 - ◆ Merchants can track/profile customers

E-Cash

- Secure
 - Single use
 - Reliable
- Low inflation
- Privacy-preserving



E-Cash Crypto Protocols

- ❖ Chaum82: blind signatures for e-cash
- ❖ Chaum88: retroactive double spender identification
- ❖ Brandis95: restricted blind signatures
- ❖ Camenisch05: compact offline e-cash
- Various practical issues:
 - Need for trusted central party
 - Computationally expensive
 - Etc.

Bitcoin



- A distributed, decentralized digital currency system
- Released by Satoshi Nakamoto 2008
- Effectively a bank run by an ad hoc network
 - Digital checks
 - A distributed transaction log

Size of the BitCoin Economy

- Number of BitCoins in circulation 11.8 million (December 2013)
- Total number of BitCoins generated cannot exceed 21 million
- Average price of a Bitcoin: around **\$300**
 - Price has been unstable.
- Total balances held in BTC 1B\$ compared with 1,200B\$ circulating in USD.
- 30 Transactions per min. (Visa transaction 200,000 per minute.)

BitCoin: Challenges

- Creation of a virtual coin/note
 - How is it created in the first place?
 - How do you prevent inflation? (What prevents anyone from creating lots of coins?)
- Validation
 - Is the coin legit? (proof-of-work)
 - How do you prevent a coin from double-spending?
- Buyer and Seller protection in online transactions
 - Buyer pays, but the seller doesn't deliver
 - Seller delivers, buyer pays, but the buyer makes a claim.
- Trust on third-parties
 - Rely on proof instead of trust
 - Verifiable by everyone
 - No central bank or clearing house

Security in Bitcoin

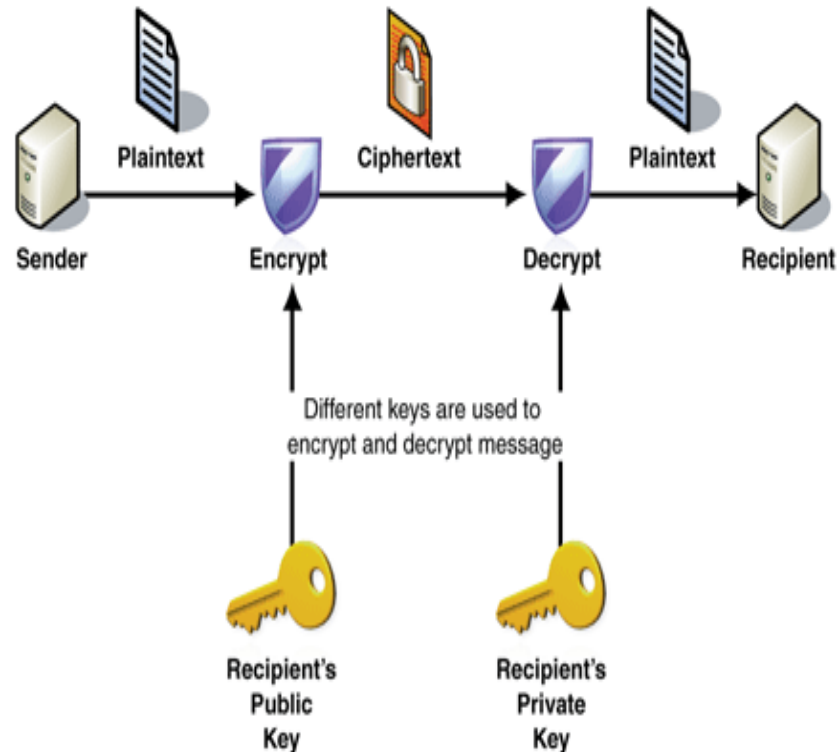
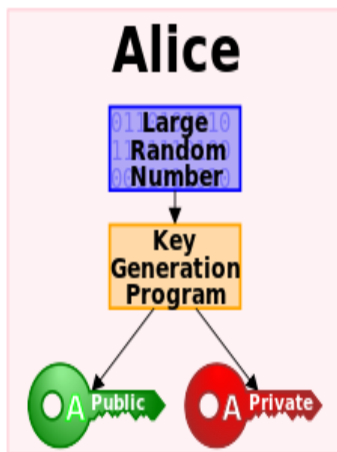
- Authentication
 - Am I paying the right person? Not some other impersonator?
- Integrity
 - Is the coin double-spent?
 - Can an attacker reverse or change transactions?
- Availability
 - Can I make a transaction anytime I want?
- Confidentiality
 - Are my transactions private? Anonymous?

Security in Bitcoin

- Authentication → **Public Key Crypto: Digital Signatures**
 - Am I paying the right person? Not some other impersonator?
- Integrity → **Digital Signatures and Cryptographic Hash**
 - Is the coin double-spent?
 - Can an attacker reverse or change transactions?
- Availability → **Broadcast messages to the P2P network**
 - Can I make a transaction anytime I want?
- Confidentiality → **Pseudonymity**
 - Are my transactions private? Anonymous?

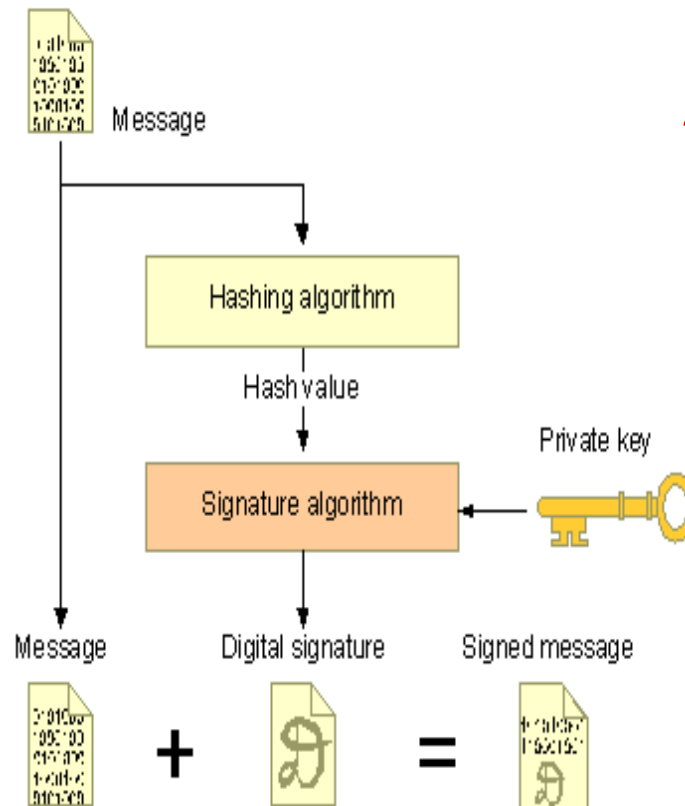
Public Key Crypto: Encryption

- Key pair: public key and private key



Public Key Crypto: Digital Signature

- First, create a message digest using a cryptographic hash
- Then, encrypt the message digest with your private key

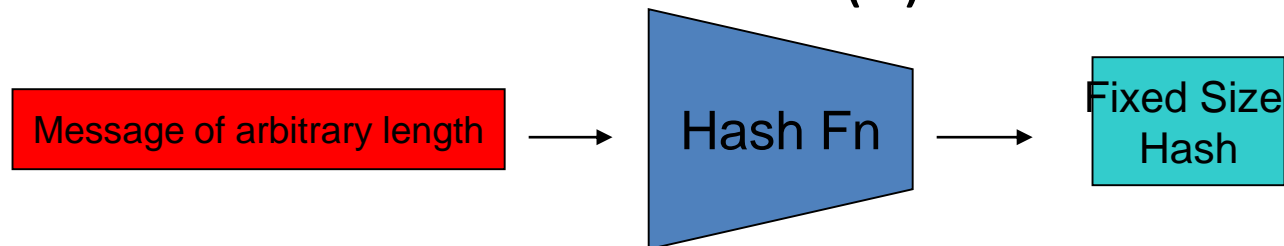


Authentication
Integrity

Non-repudiation

Cryptographic Hash Functions

- **Consistent:** $\text{hash}(X)$ always yields same result
- **One-way:** given Y , hard to find X s.t. $\text{hash}(X) = Y$
- **Collision resistant:** given $\text{hash}(W) = Z$, hard to find X such that $\text{hash}(X) = Z$



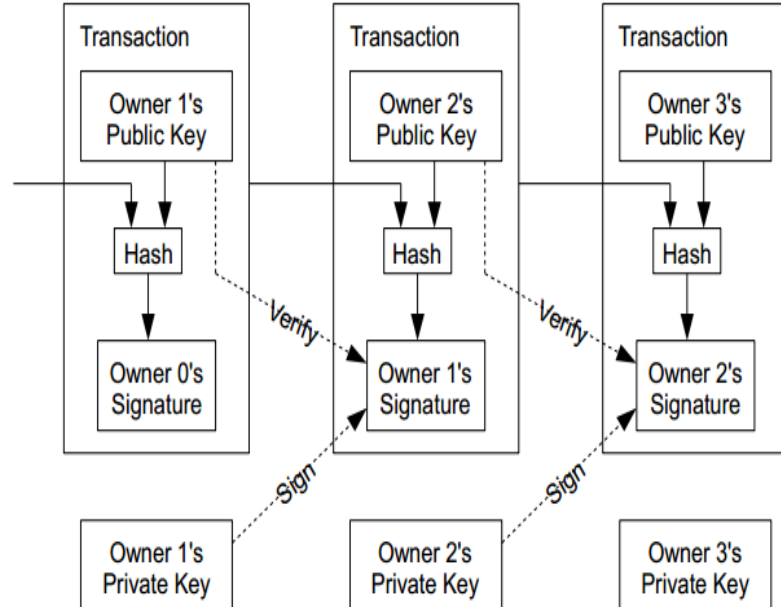
Back to BitCoin

- Validation
 - Is the coin legit? (proof-of-work) → Use of Cryptographic Hashes
 - How do you prevent a coin from double-spending? → Broadcast to all nodes
- Creation of a virtual coin/note
 - How is it created in the first place? → Provide incentives for miners
 - How do you prevent inflation? (What prevents anyone from creating lots of coins?) → Limit the creation rate of the BitCoins

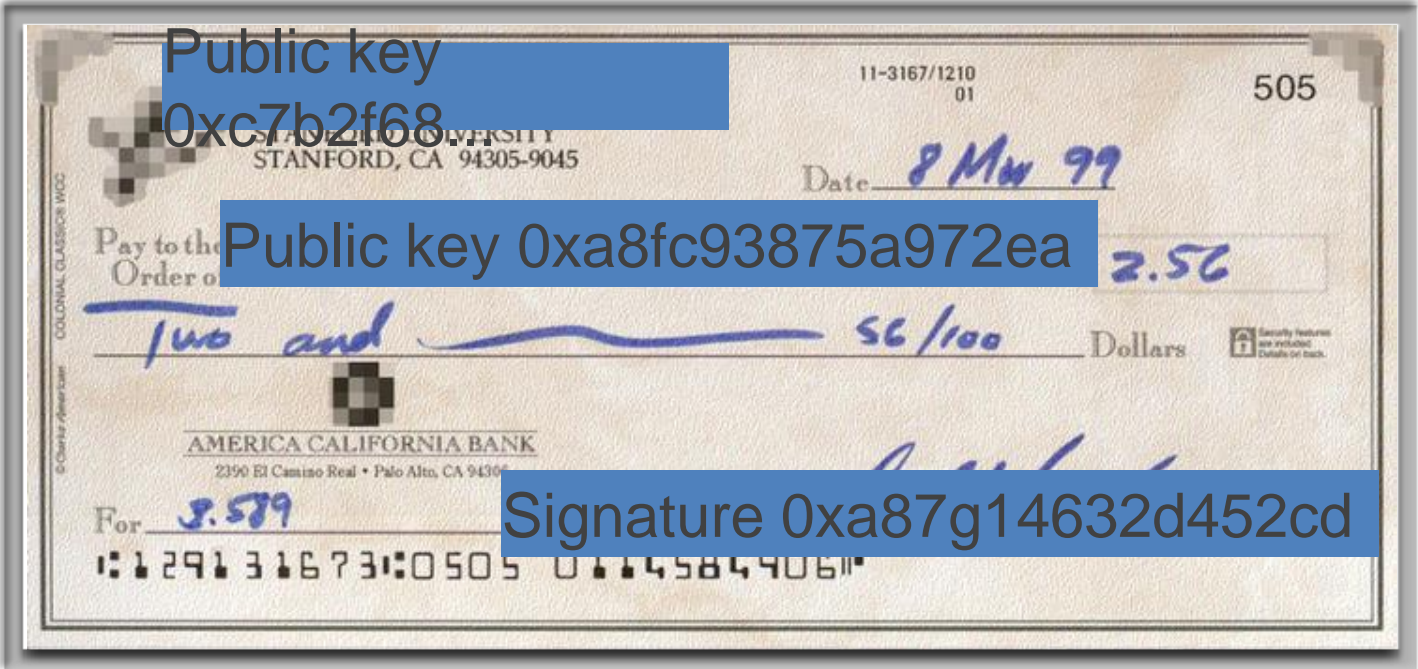
Bitcoin

- Electronic coin == chain of digital signatures
- BitCoin transfer: $\text{Sign}(\text{Previous transaction} + \text{New owner's public key})$
- Anyone can verify (n-1)th owner transferred this to the nth owner.
- Anyone can follow the history

Given a BitCoin

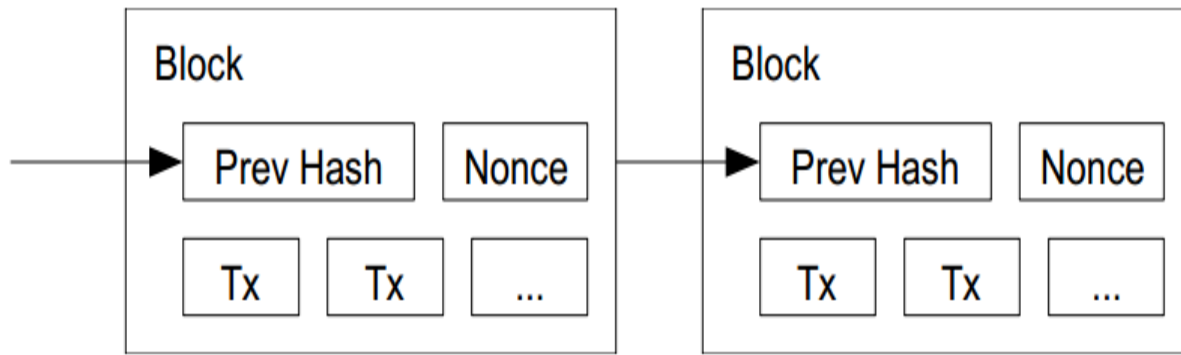


Bitcoin Transactions



Use of Cryptographic Hashes

- Proof-of-work
 - Block contains transactions to be validated and previous hash value.
 - Pick a nonce such that $H(\text{prev hash}, \text{nonce}, \text{Tx}) < E$. E is a variable that the system specifies. Basically, this amounts to finding a hash value whose leading bits are zero. The work required is exponential in the number of zero bits required.
 - Verification is easy. But proof-of-work is hard.



Preventing Double-spending

- The only way is to be aware of all transactions.
- Each node (miner) verifies that this is the first spending of the Bitcoin by the payer.
- Only when it is verified it generates the proof-of-work and attach it to the current chain.

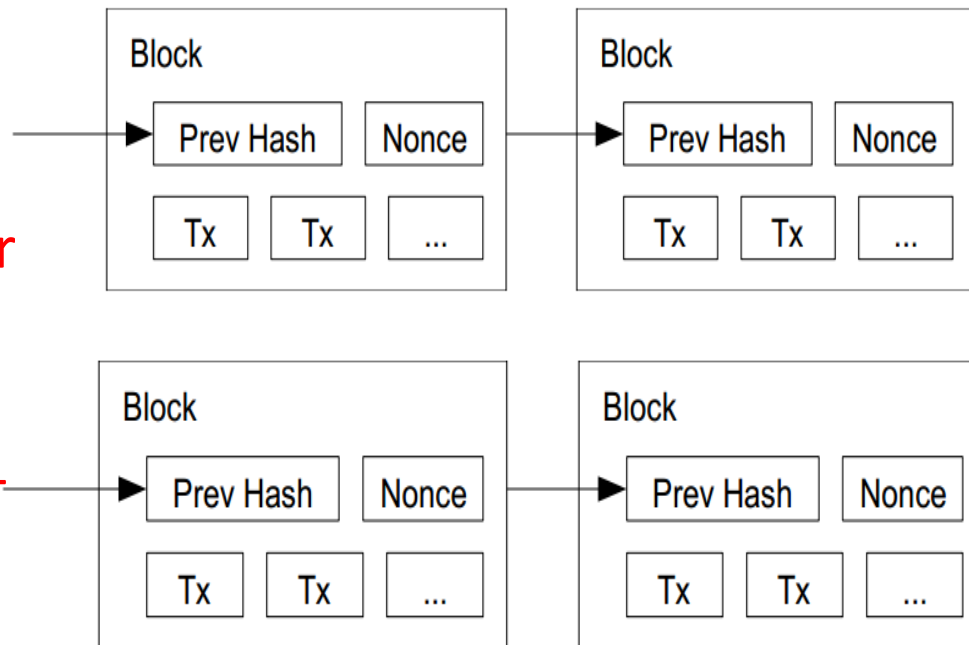
Bitcoin Network

- Each P2P node runs the following algorithm:
 - New transactions are broadcast to all nodes.
 - Each node (miners) collects new transactions into a block.
 - Each node works on finding a proof-of-work for its block. (**Hard to do. Probabilistic. The one to finish early will probably win.**)
 - When a node finds a proof-of-work, it broadcasts the block to all nodes.
 - Nodes accept the block only if all transactions in it are valid (**digital signature checking**) and not already spent (check all the transactions).
 - Nodes express their acceptance by working on creating the next block in the chain, using the hash of the accepted block as the previous hash.

Tie breaking

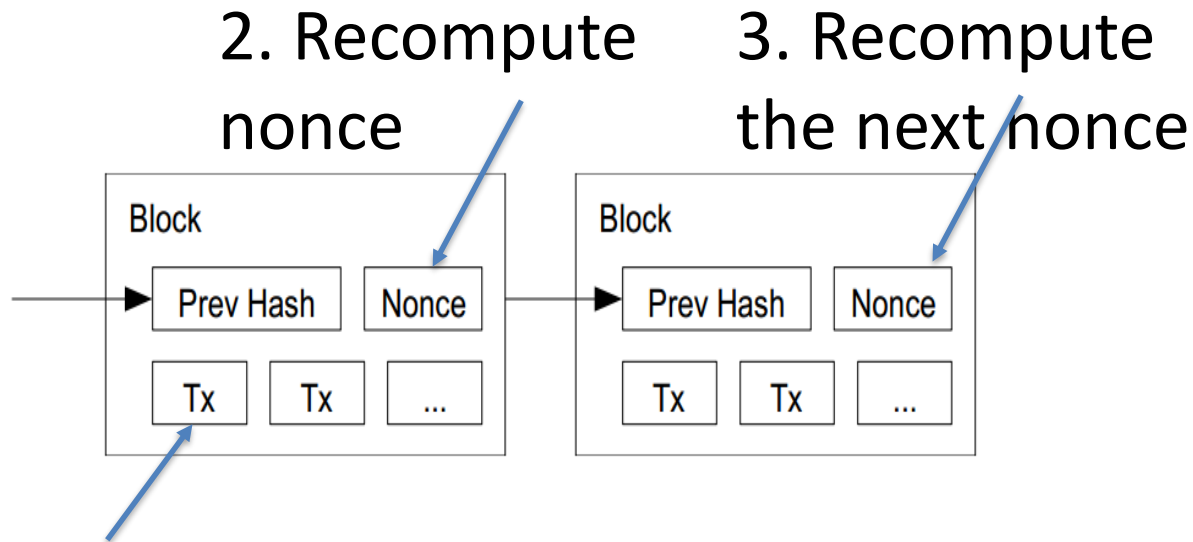
- Two nodes may find a correct block simultaneously.
 - Keep both and work on the first one
 - If one grows longer than the other, take the longer one

Two different block chains (or blocks) may satisfy the required proof-of-work.



Reverting is Hard

- Reverting gets exponentially hard as the chain grows.



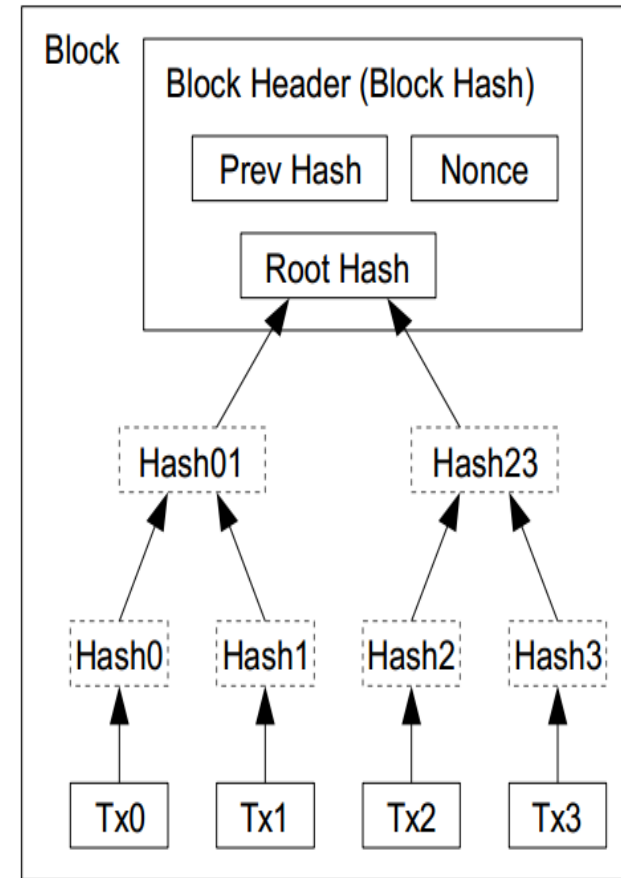
1. Modify the transaction
(revert or change the payer)

Practical Limitation

- At least 10 mins to verify a transaction.
 - Agree to pay
 - Wait for one block (10 mins) for the transaction to go through.
 - But, for a large transaction (\$\$\$) wait longer. Because if you wait longer it becomes more secure. For large \$\$\$, you wait for six blocks (1 hour).

Optimizations

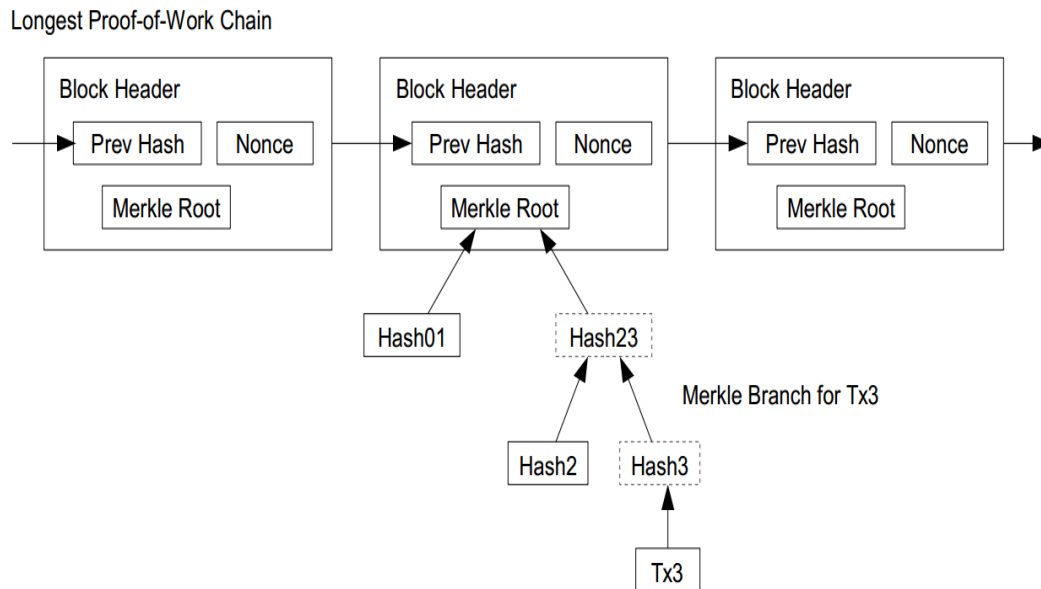
- Merkle Tree
 - Only keep the root hash
 - Delete the interior hash values to save disk
 - Block header only contains the root hash
 - Block header is about 80 bytes
 - $80 \text{ bytes} * 6 \text{ per/hr} * 24 \text{ hrs} * 365 = 4.2 \text{ MB/year}$
 - Why keep use a Merkle tree?



Transactions Hashed in a Merkle Tree

Simplified payment verification

- Any user can verify a transaction easily by asking a node.
- First, get the longest proof-of-work chain
- Query the block that the transaction to be verified (tx3) is in.
- Only need Hash01 and Hash2 to verify; not the entire Tx's.



BitCoin Economics

- Rate limiting on the creation of a new block
 - Adapt to the “network’s capacity”
 - A block created every 10 mins (six blocks every hour)
 - How? Difficulty is adjusted every two weeks to keep the rate fixed as capacity/computing power increases
- N new Bitcoins per each new block: credited to the miner → incentives for miners
 - N was 50 initially. In 2013, N=25.
 - Halved every 210,000 blocks (every four years)
 - Thus, the total number of BitCoins will not exceed 21 million. (After this miner takes a fee)

Privacy Implications

- No anonymity, only pseudonymity
- All transactions remain on the block chain—
indefinitely!
- Retroactive data mining
 - Target used data mining on customer purchases to identify pregnant women and target ads at them (NYT 2012), ended up informing a woman's father that his teenage daughter was pregnant
 - Imagine what credit card companies could do with the data

Zerocoin

- A distributed approach to private electronic cash
- Extends Bitcoin by adding an anonymous currency on top of it
- Zerocoins are exchangeable for bitcoins

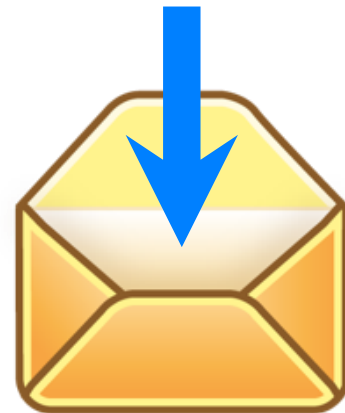
What is a zerocoin?

A zerocoin is:

Economically: a promissory note redeemable for a bitcoin

Cryptographically: an opaque envelope containing a serial number used to prevent double spending

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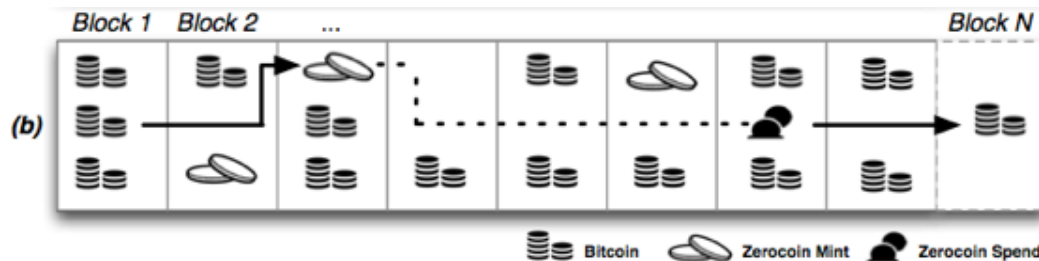
Commitments

- Allow you to commit to and later reveal a value
- Binding: value cannot be tampered with
- Blinding: value cannot be read until revealed



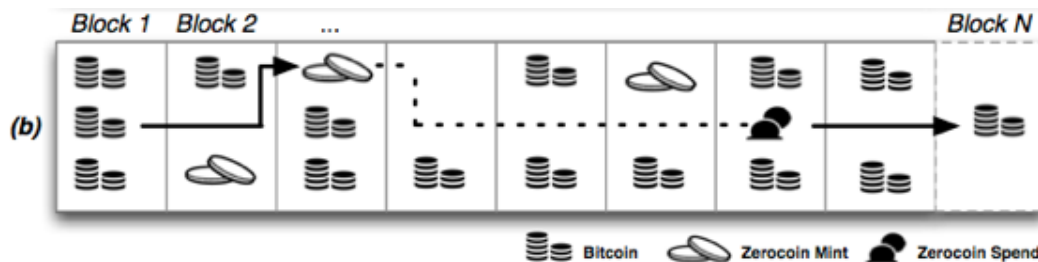
Zerocoins: where do they come from?

- Anyone can make one
- Choose a random serial number and commit to it
- Mint a zerocoin by putting a mint transaction in the block chain which “spends” a bitcoin and includes the commitment
- Spending a zerocoin gives the recipient a bitcoin



Zerocoins: ...and where do they go?

- The “spent” bitcoins end up escrowed
- To spend a zerocoin
 - You reveal the serial number
 - Prove it is from some zerocoin in the block chain
 - Put the spent serial number in the block chain



Zero-knowledge proofs

- Zero-knowledge [Goldwasser, Micali 1980s, and beyond]
- Prove knowledge of a witness satisfying a statement
- Specific variant: non-interactive proof of knowledge
- Here we prove we know:
 1. The serial number of a zerocoin
 2. That the coin is in the block chain

Zero-knowledge proof

- Inefficient approach
 - Identify all valid zerocoins in the block chain (call them $C_1 \dots C_N$)
 - Prove that S is the serial number of a coin C and $C = C_1 \vee C = C_2 \vee \dots \vee C = C_N$
 - This “OR” proof is $O(N)$
- Zerocoin uses cryptographic accumulators
 - Sublinear

Zerocoin protocol

Generate a commitment to a random serial number S :

$$\textcircled{C} = g^s h^r \text{ mod } q \quad \text{where } \textcircled{C} \text{ prime}$$

(Store serial number S and randomness r)

Accumulate all valid coins, compute witness w_i

Reveal S and prove knowledge of witness to commitment accumulation and its randomness r

Discussion

- The future of Bitcoin?
- Attacks on Zerocoin?
- Should we tradeoff privacy for usability? Is privacy a main principle?

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