



Tashkent State University of Economics

**Household finance**

Lecture 4: Households risk preferences.

Lecturer: professor Otabek Karshiev

# PORTFOLIO THEORY AND RISK

Note that only a selection of these slides will be dealt with in detail, in the lecture

All other slides are there to guide you towards the key points in Cuthbertson/Nitzsche “Investments” and in the end of chapter questions

Revise your elementary stats before the lecture

# 'Active' versus 'Passive' Strategy

3

- Sharpe Ratio for any portfolio-k

- $$S_k = (ER_k - r) / \sigma_k$$

- Active portfolio managers must try and beat the Sharpe ratio of the 'passive' investment strategy (i.e. holding the market portfolio, month in-month-out).

- $ER_k$  = average of 'out-turn' values for monthly portfolio returns (net of transactions costs) over say 3 years, for any portfolio-k and any 'strategy' (e.g. trying to pick winners)

- $\sigma_k$  = sample SD of these monthly returns (over 3 years)

- Compare investment strategies:

- The investor with the highest value of  $S_k$  is the 'winner'

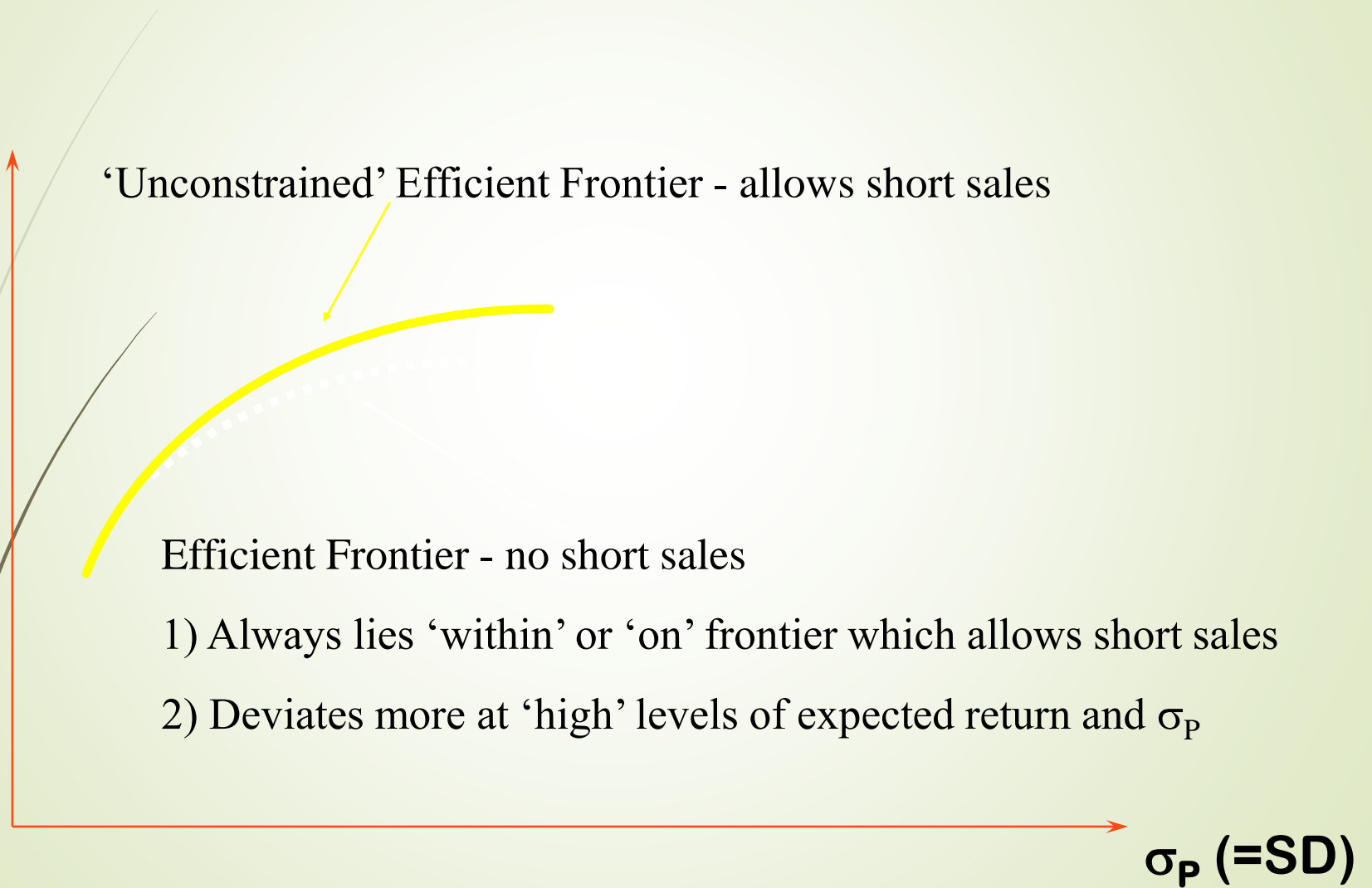
# Practical Issues

4

- 1) Suppose all investors do not have the same views about expected returns and covariances.
  - ~ we can still use our methodology to work out **optimal proportions/weights** for for each individual investor.
- 2) The optimal weights will change as forecasts of returns and correlations change - the 'passive' portfolio needs 'some rebalancing' - 'Tracking Error'
- 3) The method can be easily adopted to include transactions costs of buying and selling, and investing "new" flows of money.
- 4) Lots of weights might be negative, which implies **short-selling**, possibly on a large scale. If this is 'impractical' you can re-calculate, where all the **weights are forced to be positive**.

# No-Short Sales Allowed

5 (ie. All 'weights' > 0 )



# Practical Issues

6

- ▶ 5) The optimal weights depend on estimate/forecasts of expected returns and covariances.
- ▶ If these **forecasts are incorrect**, the actual risk-return outcome may be very different from that envisaged when you started out
- ▶ Put another way a **small change in expected returns** can radically alter the optimal weights - ie. **Extreme sensitivity** to the "inputs".
- ▶ The optimal weights are **relatively insensitive** to errors in forecasts of **correlations and variances** - hence some investors choose weights to min. SD only.

# International Diversification

7

- Within a particular country, either portfolio theory will be used to guide proportions in each industrial sector, or they will try just 'track' the respective domestic indices (e.g. the S&P500, FTSE 100).
- There is some evidence that INVESTMENT COMMITTEES are moving towards choosing industrial sector weights, subject to limits on the resulting country proportions. This is to 'gain' from the disparate business cycles between industries (e.g. world car industry has different cycle to world chemicals)
- This is because 'country indices' are beginning to have 'high correlations' (e.g. US and UK aggregate business cycles are now more highly correlated).

# International Diversification

8

- ▶ TACTICAL ASSET\_ALLOCATION
- ▶ Use part of funds for market timing' the business cycle'
- ▶ (e.g. switch 10% of speculative funds out of US and into SE Asia )
- ▶ -might use a macro-economic model for forecasts
- ▶ -does not easily 'fit' into portfolio theory because usually little or no formal estimate of risk is made

## SELF STUDY SLIDES

The following slides provide a simple numerical example to construct the efficient frontier, the capital market line and the market portfolio

These slides will NOT be covered in the lectures

# STATISTICS REVISION: Some Definitions

0

## Expected Return of Portfolio

➤  $E(R_p) = w_1 ER_1 + w_2 ER_2$

## Variance of Portfolio

➤  $\sigma_p^2 = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2 w_1 w_2 \sigma_{12}$

➤  $\sigma_p^2 = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2 w_1 w_2 (\rho \sigma_1 \sigma_2)$



➤ Also, 'proportions' are:  $w_1 + w_2 = 1$ .

➤ Note  $\sigma_{12} = \rho \sigma_1 \sigma_2$  - from statistics

➤ The above are used to derive the EFFICIENT FRONTIER by (arbitrarily) altering the w's

# STAGE 1: 2 Risky Assets: Real world data (statistician)

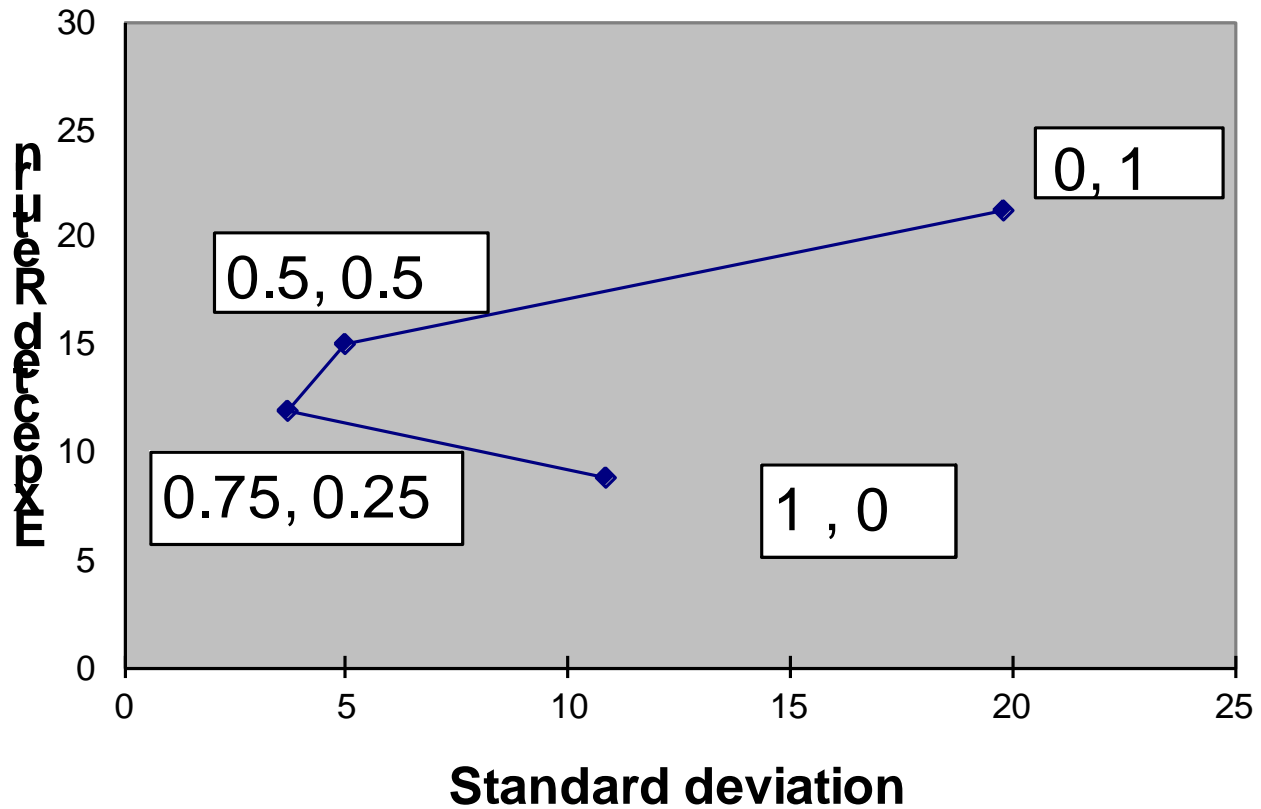
	Risky Assets	
	Equity-1	Equity-2
Mean, $ER_i$	8.75	21.25
$\sigma_i$ (SD) .	10.83	19.80
<b>Correlation (Equity-1, Equity-2): - 0.9549</b>		
<b>Cov(Equity-1, Equity-2) : -204.688</b>		

STAGE 1: Construct Efficient Frontier  
(Choose different  $w$ 's and calculate  $ER_p$  and  $\sigma_p$  combinations)

State	Shares of		Portfolio	
	Equity-1	Equity-2	$ER_p$	$\sigma_p$
	$w_1$	$w_2$		
1	1	0	8.75	10.83
2	0.75	0.25	11.88	3.70
3	0.5	0.5	15	5
4	0	1	21.25	19.80

Now plot values of  $ER_p$  and  $\sigma_p$  and construct the Efficient Frontier

# Efficient Frontier



# Efficient Frontier with 'n' - Risky Assets

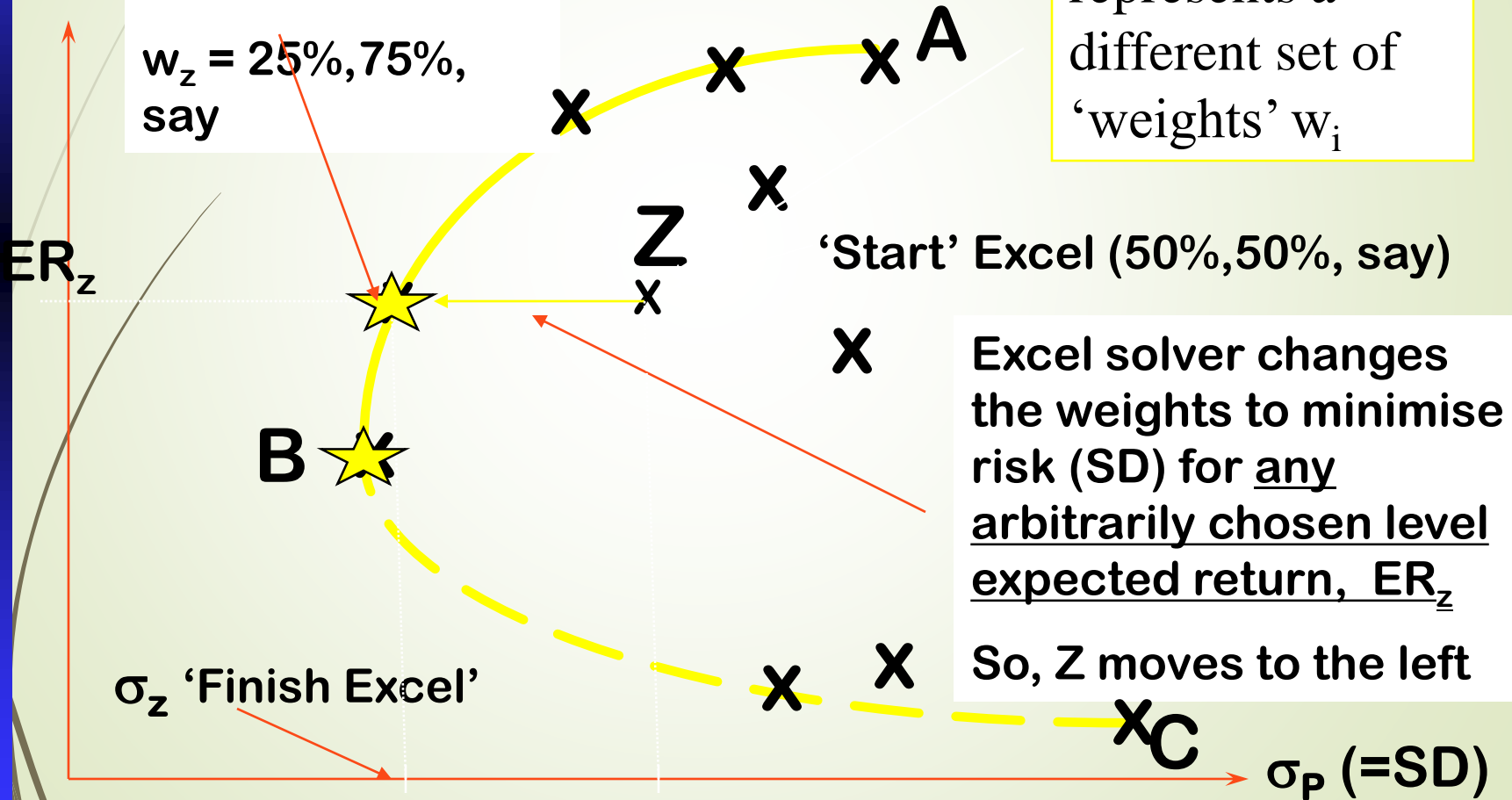
4

You require EXCEL 'SOLVER' to 'draw' the EFFICIENT FRONTIER (=A-B)

End of Excel  
minimisation

$w_z = 25\%, 75\%$ ,  
say

Each 'cross'  
represents a  
different set of  
'weights'  $w_i$



# STAGE 2: Transformation Line

5

- ▶ We have 'constructed' the efficient frontier
- ▶ Now introduce a "safe asset"
- ▶ What does the risk-return "trade-off" look like when we
- ▶ allow borrowing or lending at the safe rate
- ▶ and
- ▶ we combine this with any 'single bundle' of risky assets?
- ▶ 'New Portfolio' = 1-safe asset + 1 "bundle of risky assets"
- ▶
- ▶ Answer = Straight Line relationship between ER and  $\sigma$

# STAGE 2: Transformation Line

6

What is a 'Risky Asset bundle' ?:

- ▶ Keep (arbitrary) fixed weights in risky assets
- ▶ eg. 20% in asset-1, 80% in asset-2
- ▶ So, if you have  $W_0 = \$100$  you will hold \$20 in
- ▶ asset-1 and \$80 in asset-2
  
- ▶ Assume this gives rise to a fixed "bundle" of risky
- ▶ assets" called "q" with  $ER_q = 22.5\%$  and  $s_q = 24.8\%$
  
- ▶ Now combine 'fixed risky bundle' with the safe asset
- ▶ by borrowing/lending different \$ amounts of safe asset

# Construct 'One' Transformation Line Data

	Return	
	T-bill (safe)	Equity (Risky)
<b>Mean</b>	$r = 10$	$R_q = 22.5$
<b>Std. Dev.</b>	0	$\sigma_q = 24.87$

## FORMULAE FOR EXPECTED RETURN AND SD OF 'NEW' PORTFOLIO

$N$  = "new" portfolio of: 'safe + risky 'bundle'

$\sigma_q^2$  = variance of the risky 'bundle'

$x$  = proportion held in 'risky asset'

$(1-x)$  = proportion held in safe asset (with  $\sigma = 0$ )

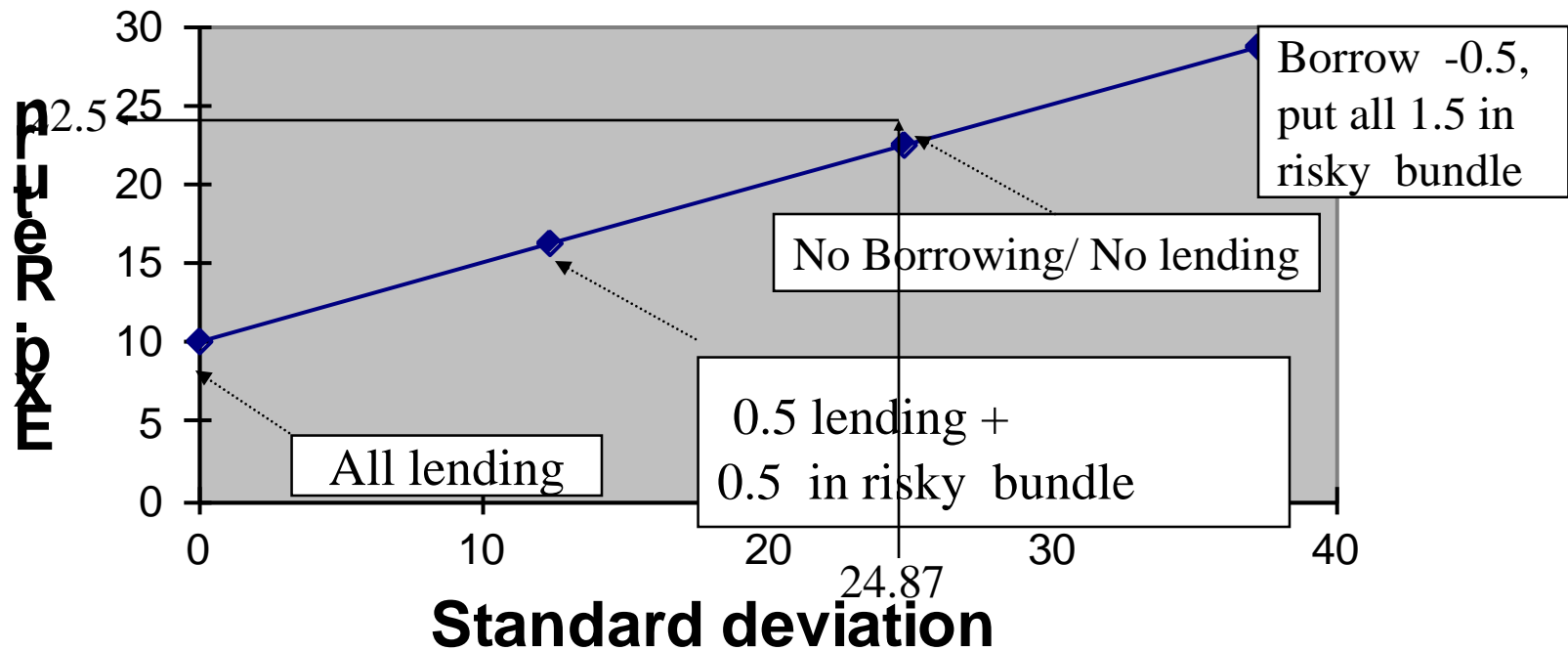
**Expected Return:**  $E(R_N) = (1-x) \cdot r + x ER_q$

**THEN: Variance (SD) of NEW PORTFOLIO** of "1-safe + 1 risky asset"

$$\sigma_N^2 = x^2 \sigma_q^2 \quad \text{OR} \quad \sigma_N = x \sigma_q$$

# Transformation Line

1 safe asset + 1 risky "bundle"



Note: At "no borrow/lend" position, ER and  $\sigma$  of "new" portfolio equals that for the risky asset alone (not surprisingly)

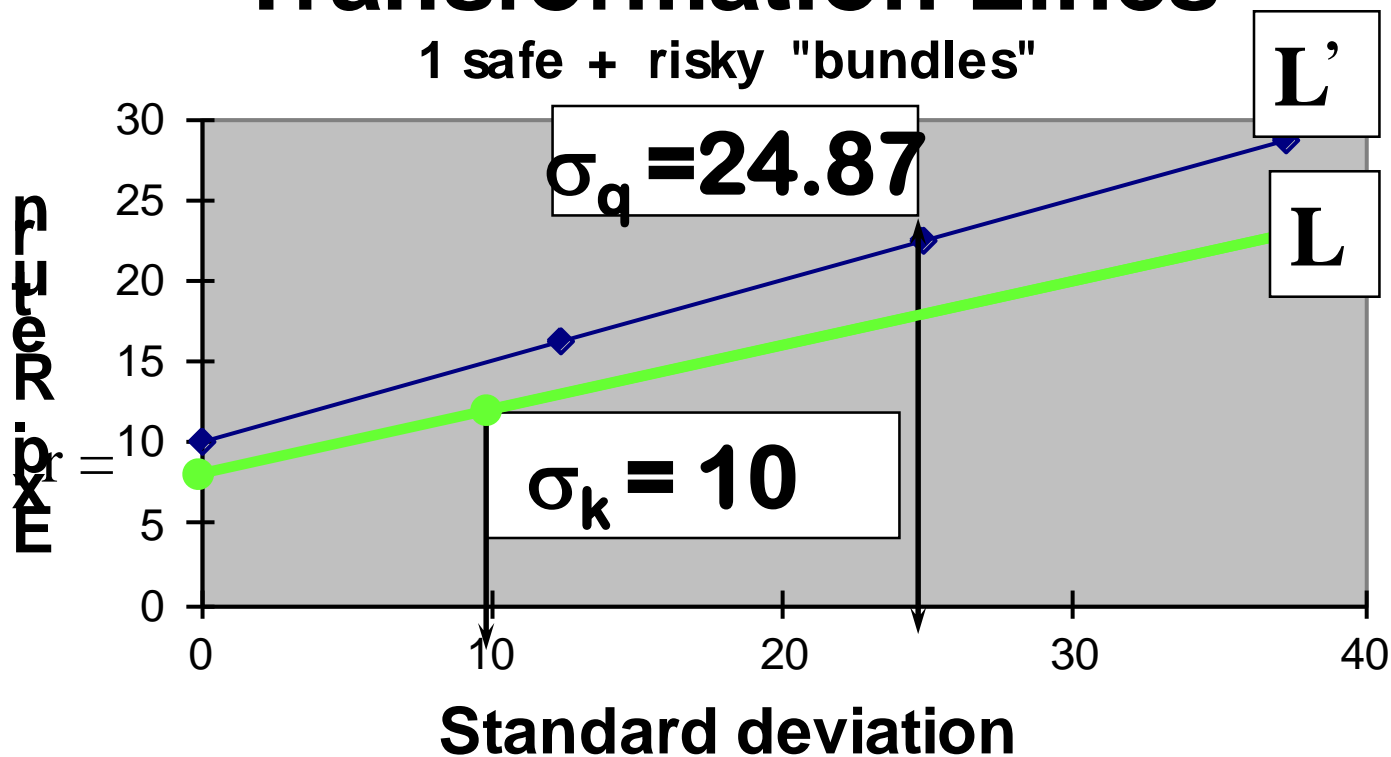
# Transformation Lines

9

- ▶ Safe asset plus ANY ONE 'arbitrary' risky bundle,
- ▶ gives a specific transformation line (which is straight
- ▶ line) between  $r$  and the s.d of the risky bundle
  
- ▶ Every single, risky bundle has its own transformation
- ▶ line
  
- ▶ Which transformation line is "best"?
  
- ▶ "THE HIGHEST ACHIEVABLE" = Capital Market Line

# Transformation Lines

1 safe + risky "bundles"

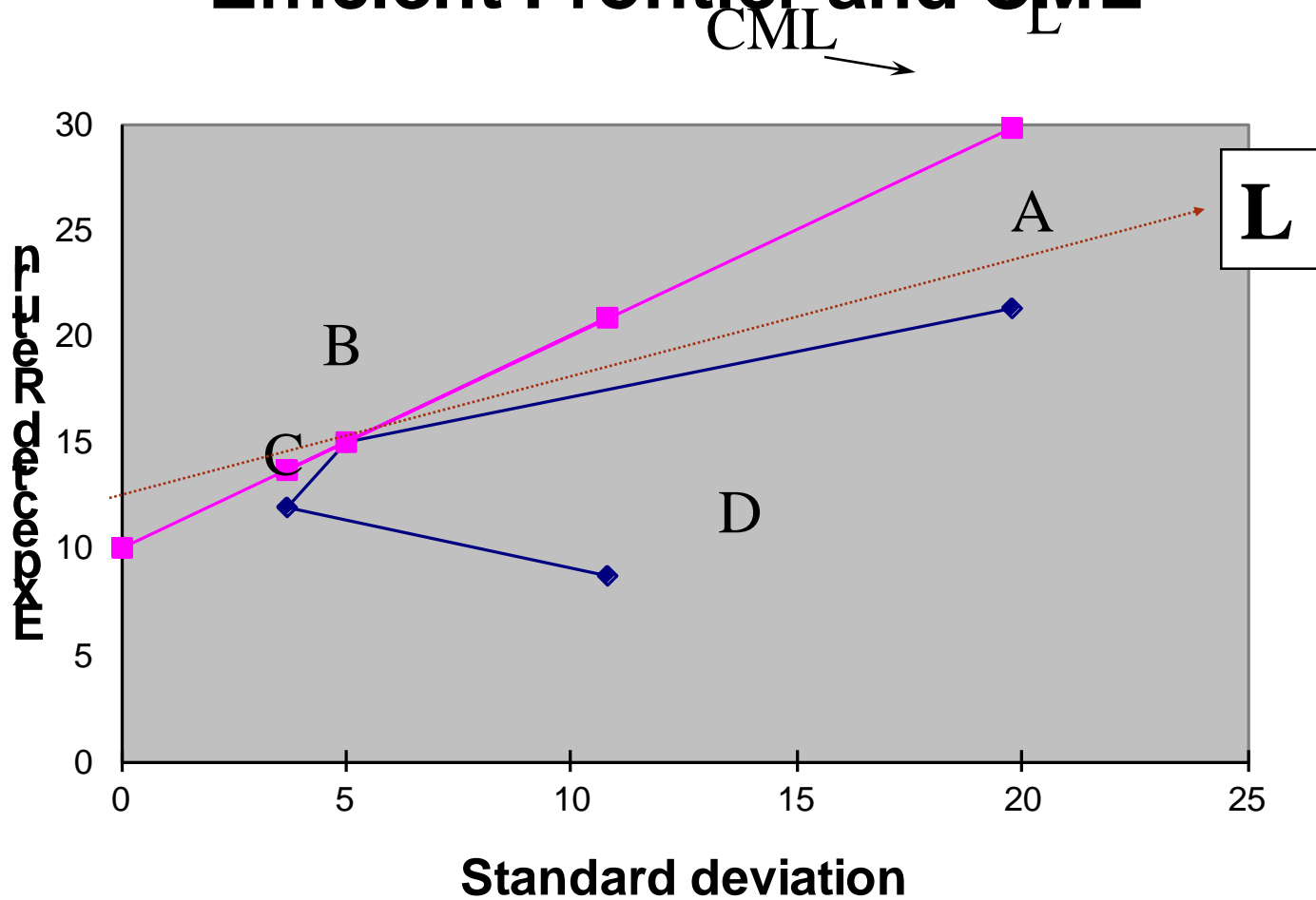


q and k are both 'points' on the efficient frontier. So q might represent (20%,80%) in risky assets and k might represent (70%,30%). Each "fixed weight" risky bundle has its own transformation

line

“B” is highest attainable transformation line, while still remaining on the efficient frontier. ‘B’ represents the optimal weights (50%,50%) for the risky bundle.

## Efficient Frontier and CML



# Market Portfolio

2

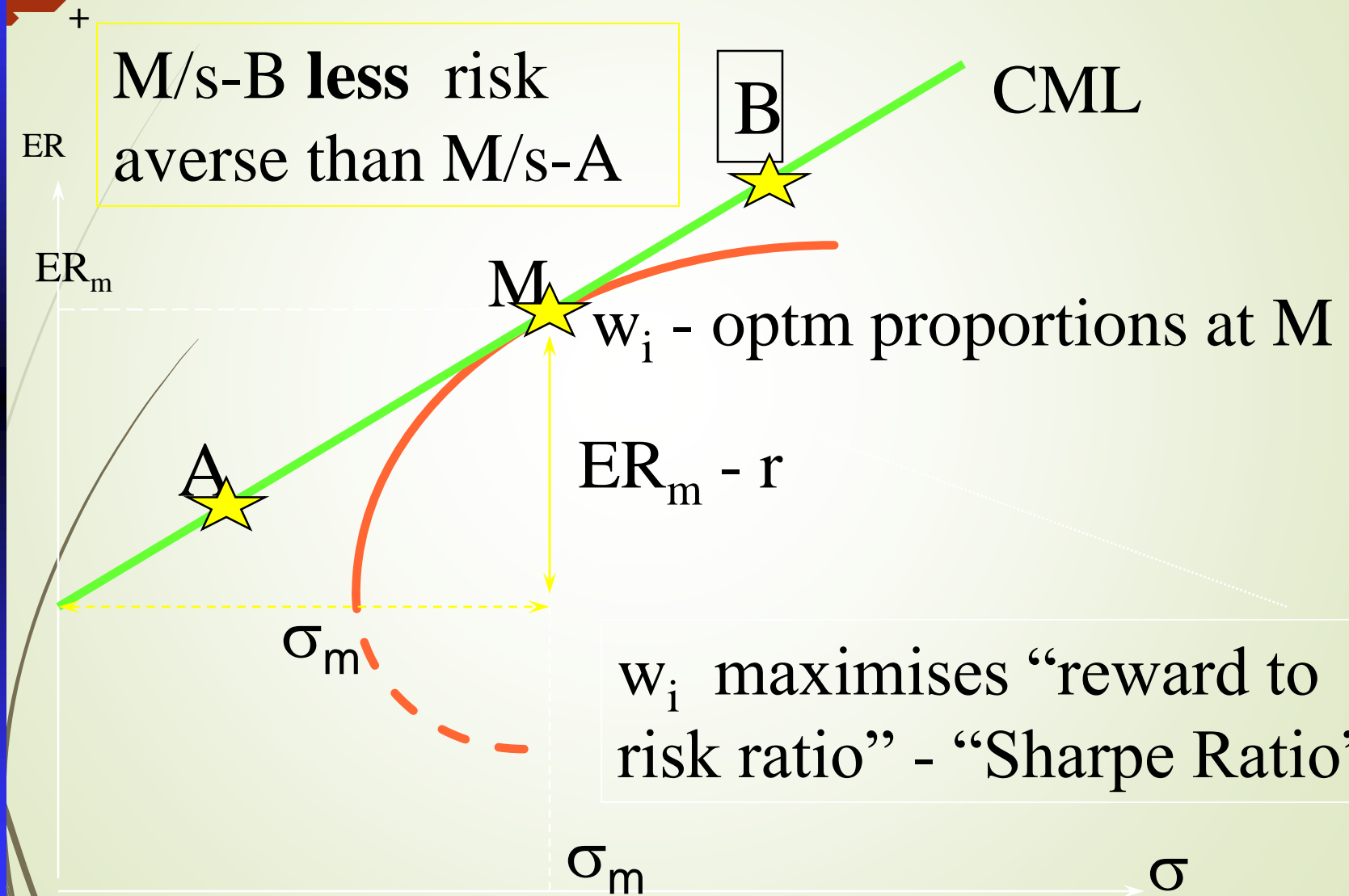
Point-B is therefore a rather special portfolio and hence is known as the “**Market Portfolio**” (as indicated by the subscript ‘m’ in the next slide)

IF everyone has the same expectations about returns, standard deviation and correlations then:

Everyone chooses point-B (which here gives 50%, 50% held in each risky asset)

# CML and Market Portfolio (M)

23



END OF SLIDES