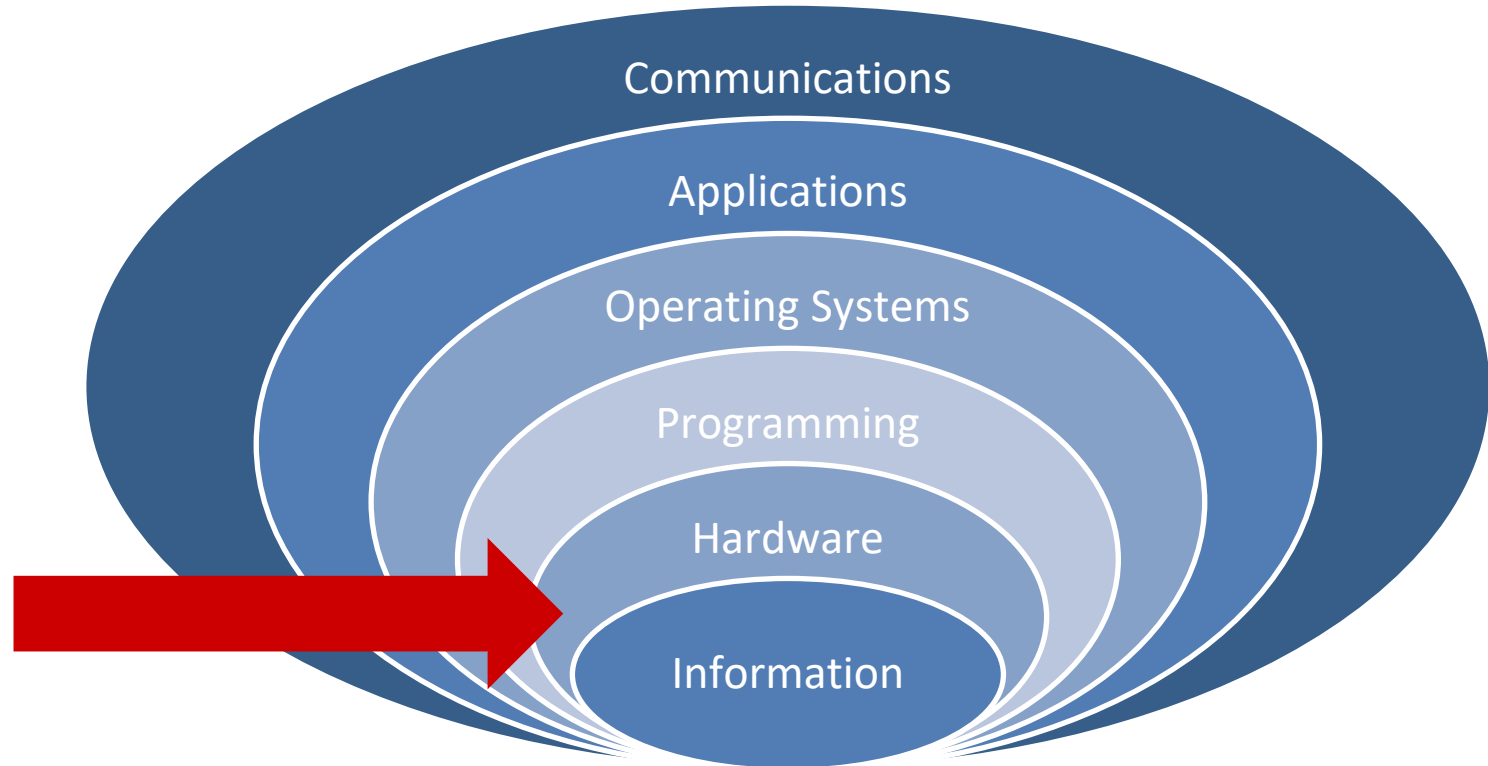


Computer Science Fundamentals

Lecture topic: Gates and Circuits

Lecturer: Olga Yugay

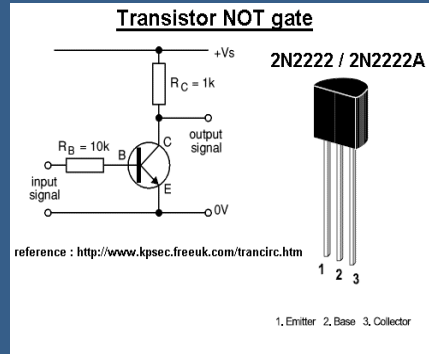
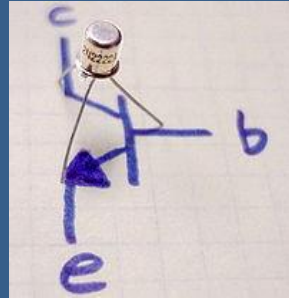
Today's focus



Today's focus

Hardware

Logic gates



Agenda

- Explore how computers use electric signals to represent and manipulate binary values
 - basic gates
 - gates combined into circuits
 - behavior gate using Boolean expressions, truth tables, and logic diagrams
 - compare and contrast a half adder and a full adder
- Python

Why study about circuits? Inside the microchip

[Khan Academy and Code.org | Circuits & Logic](#)¹

¹ Khan Academy and Code.org, 2018, Circuits & Logic. [online] Available at: < <https://youtu.be/Sc3lh3D4rCw> >

Some background

Background

- Logic gates are the **building blocks**
- Anything from small toys to supercomputers will have digital gates in them (phones, washing machines, lifts and etc.)
- Whenever a decision needs to be taken based on some inputs, a logic gate can be designed and used

Background

- Major computer components rely on logic gates
 - Arithmetic and Logic Unit
 - Primary memory a.k.a RAM (Random Access Memory)
 - Even secondary memory is now switching to using integrated circuits -> SSD (Solid State drives)³

³ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 4

Background

- What are Computers?
 - **electronic** devices;
 - the most fundamental **hardware elements** of a computer **control the flow of electricity**.

Electronic signal, 0s and 1s

- Any given electronic signal has a level of voltage.

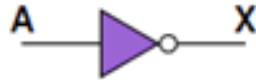
voltage level 0 to 2 volts	voltage level 2 to 5 volts
“low”	“high”
binary 0	binary 1

- Signals in a computer are constrained to be within one range or the other.⁴

⁴ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 4

Basic hardware

- **Gate** - A device that performs a basic operation on electrical signals, accepting one or more input signals and producing a single output signal
 - There are **six** most fundamental types
 - Each type of gate performs a **particular logical function**.⁵



⁵ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 4

Basic hardware

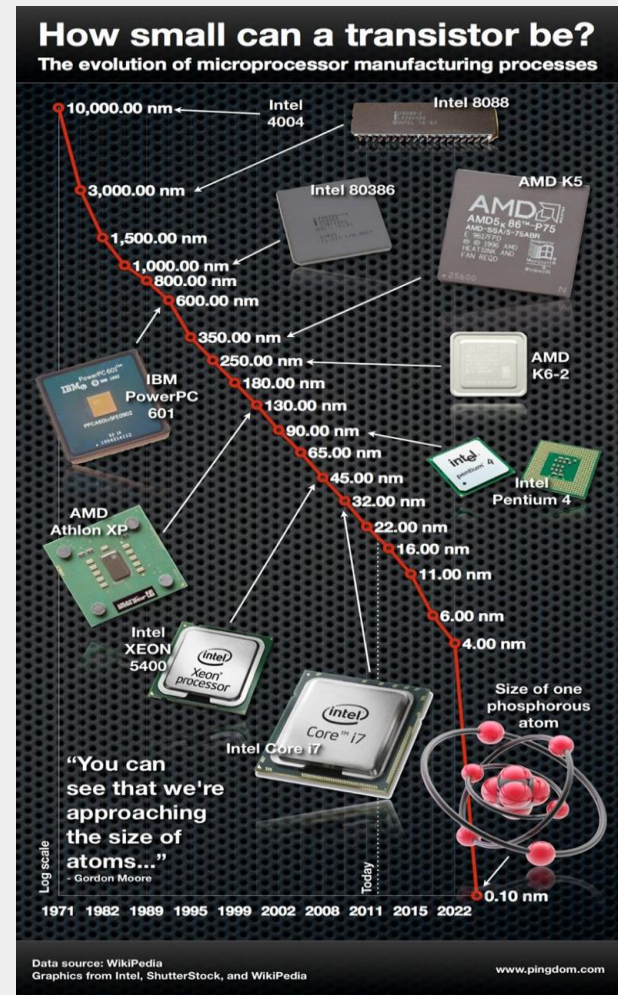
- **Circuit** - A combination of **interacting gates** designed to accomplish a specific logical function
 - circuits can be designed to **perform arithmetic** and to **store values**.
 - the output value of one gate often serves as an input value for one or more other gates.
 - The flow of electricity through a circuit is controlled by the carefully designed logic of the interacting gates. ⁶

"The number of transistors incorporated in a chip will approximately double every 24 months."

—Gordon Moore, Intel co-founder

Transistor

- Transistor is basic hardware used to build the logic gates
- * **nm, nanometer** is one millionth of a millimeter
- In **2012** a team of researchers in Australia has managed to create a transistor that is the **size of an atom**.⁷



⁷ Pingdom, S., 2012. The single-atom transistor is here – the amazing evolution of microprocessors. [Blog] TECH MUSINGS, Available at: <<https://www.pingdom.com/blog/the-single-atom-transistor-is-here-the-amazing-evolution-of-microprocessors-infographic/>>

Transistor

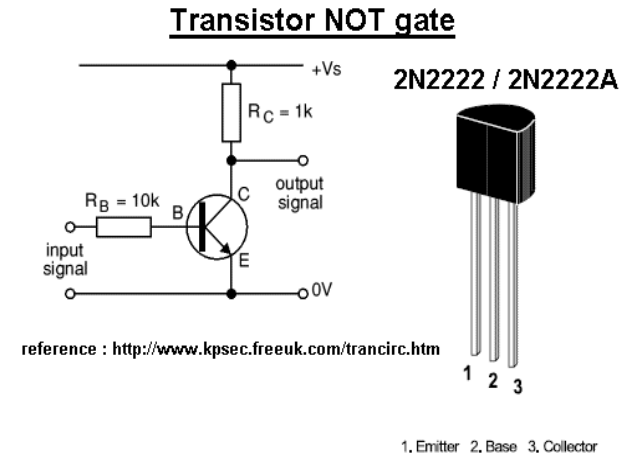
- Transistor - A device that acts either as a wire or a resistor, depending on the voltage level of an input signal
 - Semiconductor - material such as silicon that is neither a good conductor nor a good insulator⁸



FIGURE 1.6 A vacuum tube
© SPPhoto/Shutterstock



FIGURE 1.7 A transistor,
which replaced the
vacuum tube
Courtesy of Dr. Andrew Wylie.



Transistors Explained - How transistors work

- [Transistors Explained - How transistors work](#)⁹

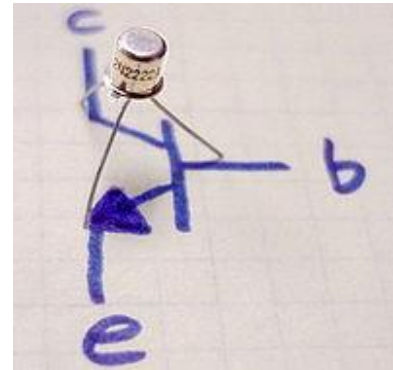
Arduino

- [Top 10 Arduino projects for beginners to advance](#)
- <https://www.arduino.cc/en/Guide/Introduction>

⁹The Engineering Mindset, 2021, *Transistors Explained - How transistors work*. [online] Available at: https://www.youtube.com/watch?v=J4oO7PT_nzQ >

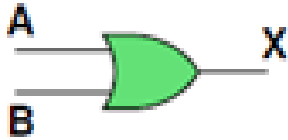
Gates and Circuits: Notational methods

- There are three different, but equally powerful, **notational** methods for describing the behavior of gates and circuits:
 1. Boolean expressions
 2. Logic diagrams
 3. Truth tables ⁸



Example: OR gate⁹

1. $X=A+B$



2.

Truth Table

A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

3.

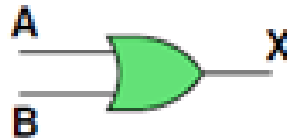
1. Boolean algebra: Boolean expressions¹⁰

- An English mathematician named George Boole invented a form of algebra in which variables and functions take on only one of two values (0 and 1).
- Specific operations and properties in Boolean algebra allow us to define and manipulate circuit logic using a mathematical notation.
- OR gate boolean expression: $X=A+B$

¹⁰ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 4

2. Logic diagram ¹¹

- ...is a graphical representation of a circuit. Each type of gate is represented by a specific graphical symbol.
- By connecting those symbols in various ways we can visually represent the logic of an entire circuit.
- **OR gate logic diagram:**



3. Truth table ¹²

- defines the function of a gate by listing all possible input combinations that the gate could encounter, and the corresponding output.
- **OR gate truth table:**

Truth Table

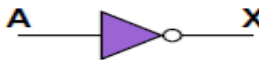
A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

6 most fundamental gate types

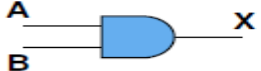
- NOT
- AND
- OR
- XOR
- NAND
- NOR

6 most fundamental gate types¹³

NOT gate inverts its single input value.

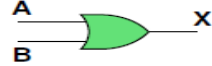
Boolean Expression	Logic Diagram Symbol	Truth Table						
$x = \overline{A}$		<table border="1"><thead><tr><th>A</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>1</td></tr><tr><td>1</td><td>0</td></tr></tbody></table>	A	X	0	1	1	0
A	X							
0	1							
1	0							

AND gate produces 1 if both input values are 1.

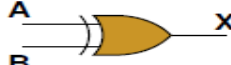
Boolean Expression	Logic Diagram Symbol	Truth Table															
$x = AB$		<table border="1"><thead><tr><th>A</th><th>B</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></tbody></table>	A	B	X	0	0	0	0	1	0	1	0	0	1	1	1
A	B	X															
0	0	0															
0	1	0															
1	0	0															
1	1	1															

6 most fundamental gate types ¹⁴

OR gate produces 1 if one or the other or both input values are 1.

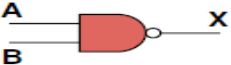
Boolean Expression	Logic Diagram Symbol	Truth Table															
$x = A + B$		<table border="1"><thead><tr><th>A</th><th>B</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>1</td></tr></tbody></table>	A	B	X	0	0	0	0	1	1	1	0	1	1	1	1
A	B	X															
0	0	0															
0	1	1															
1	0	1															
1	1	1															

XOR gate produces 1 if one or the other (but not both) input values are 1.

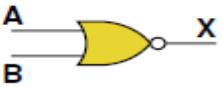
Boolean Expression	Logic Diagram Symbol	Truth Table															
$x = A \oplus B$		<table border="1"><thead><tr><th>A</th><th>B</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></tbody></table>	A	B	X	0	0	0	0	1	1	1	0	1	1	1	0
A	B	X															
0	0	0															
0	1	1															
1	0	1															
1	1	0															

6 most fundamental gate types ¹⁵

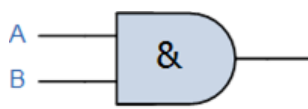
NAND gate produces the opposite results of an AND gate.

Boolean Expression	Logic Diagram Symbol	Truth Table															
$x = \overline{AB}$		<table border="1"><thead><tr><th>A</th><th>B</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>1</td></tr><tr><td>1</td><td>0</td><td>1</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></tbody></table>	A	B	X	0	0	1	0	1	1	1	0	1	1	1	0
A	B	X															
0	0	1															
0	1	1															
1	0	1															
1	1	0															

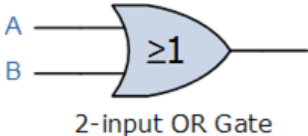
NOR gate produces the opposite results of an OR gate.

Boolean Expression	Logic Diagram Symbol	Truth Table															
$x = \overline{A + B}$		<table border="1"><thead><tr><th>A</th><th>B</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>1</td></tr><tr><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>0</td></tr></tbody></table>	A	B	X	0	0	1	0	1	0	1	0	0	1	1	0
A	B	X															
0	0	1															
0	1	0															
1	0	0															
1	1	0															

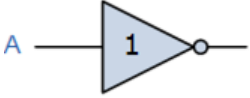
Let's practice!

Symbol	Truth Table		
 <p>2-input AND Gate</p>	A	B	X
	0	0	
	0	1	
	1	0	
	1	1	
Boolean Expression $X = AB$	Read as A AND B gives x		

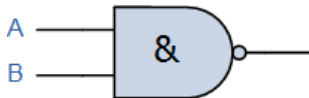
Let's practice!

Symbol	Truth Table		
 <p>2-input OR Gate</p>	A	B	X
	0	0	
	0	1	
	1	0	
	1	1	
Boolean Expression $X = A+B$	Read as A OR B gives x		

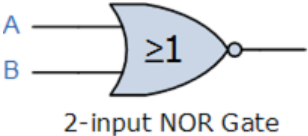
Let's practice!

Symbol	Truth Table						
	<table border="1"><tbody><tr><td>A</td><td>x</td></tr><tr><td>0</td><td></td></tr><tr><td>1</td><td></td></tr></tbody></table>	A	x	0		1	
A	x						
0							
1							
Boolean Expression $X = A'$	Read as inversion of A gives Not x						

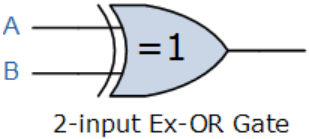
Let's practice!

Symbol	Truth Table		
 <p>2-input NAND Gate</p>	A	B	x
	0	0	
	0	1	
	1	0	
	1	1	
Boolean Expression $Q = (AB)'$	Read as A AND B gives NOT-x		

Let's practice!

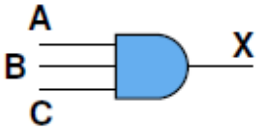
Symbol	Truth Table		
 <p>2-input NOR Gate</p>	A	B	x
	0	0	
	0	1	
	1	0	
	1	1	
Boolean Expression $x = (A+B)'$	Read as A OR B gives NOT-x		

Let's practice!

Symbol	Truth Table		
 <p data-bbox="568 642 813 671">2-input Ex-OR Gate</p>	A	B	x
	0	0	
	0	1	
	1	0	
	1	1	
Boolean Expression $Q = A \oplus B$			

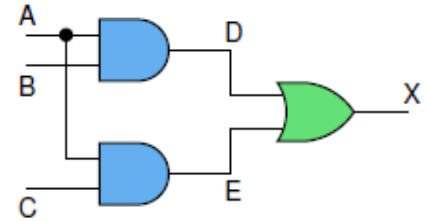
Gates with more inputs¹⁶

- Same rules apply but now to **three** inputs

Boolean Expression	Logic Diagram Symbol	Truth Table																																				
ABC		<table border="1"><thead><tr><th>A</th><th>B</th><th>C</th><th>X</th></tr></thead><tbody><tr><td>0</td><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>0</td><td>1</td><td>0</td></tr><tr><td>0</td><td>1</td><td>0</td><td>0</td></tr><tr><td>0</td><td>1</td><td>1</td><td>0</td></tr><tr><td>1</td><td>0</td><td>0</td><td>0</td></tr><tr><td>1</td><td>0</td><td>1</td><td>0</td></tr><tr><td>1</td><td>1</td><td>0</td><td>0</td></tr><tr><td>1</td><td>1</td><td>1</td><td>1</td></tr></tbody></table>	A	B	C	X	0	0	0	0	0	0	1	0	0	1	0	0	0	1	1	0	1	0	0	0	1	0	1	0	1	1	0	0	1	1	1	1
A	B	C	X																																			
0	0	0	0																																			
0	0	1	0																																			
0	1	0	0																																			
0	1	1	0																																			
1	0	0	0																																			
1	0	1	0																																			
1	1	0	0																																			
1	1	1	1																																			

Circuits¹⁷

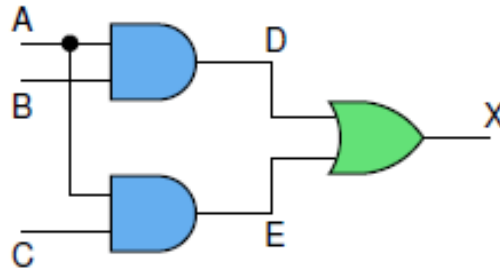
- **Combinational circuit** - A circuit whose output is solely determined by its **input values**



- **Sequential circuit** – A circuit whose output is a function of **input values** and the **current state of the circuit (usually depend on clock cycles)**
 - Normally used for storage

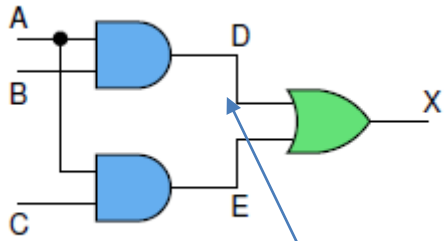
Combinatorial circuit ¹⁸

- Gates are combined into circuits by using gate output as an input to another gate



Combinatorial circuit: Example 1

Logic diagram



Truth table

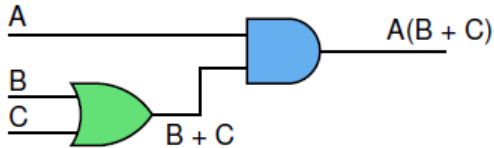
A	B	C	D	E	X
0	0	0			
0	0	1			
0	1	0			
0	1	1			
1	0	0			
1	0	1			
1	1	0			
1	1	1			

$X = (AB + AC)$
Boolean expression

Combinatorial circuit: Example 2

- Represent

$A(B + C)$ using logic diagram and truth table



A	B	C	B + C	A(B+C)
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

*as good as possible...*¹⁹

- When we build a combinatorial circuit from some kind of specification, we always try to make it ***as good as possible***.
 - In some applications, **minimize the number of gates** (or the number of transistors).
 - In other, optimize **a *delay*** (the time it takes a signal to traverse the circuit) , or ***low power consumption***.
- In general, a mixture of such criteria must be applied.

Circuit equivalence ²⁰

- **Circuit equivalence** - The same output for each corresponding input value combination for two circuits

- $A(B+C) = AB + AC$

Few properties of Boolean algebra ²¹

PROPERTY	AND	OR
Commutative	$AB = BA$	$A + B = B + A$
Associative	$(AB)C = A(BC)$	$(A + B) + C = A + (B + C)$
Distributive	$A(B + C) = (AB) + (AC)$	$A + (BC) = (A + B)(A + C)$
Identity	$A1 = A$	$A + 0 = A$
Complement	$A(A') = 0$	$A + (A') = 1$
De Morgan's law	$(AB)' = A' \text{ OR } B'$	$(A + B)' = A'B'$

What is the most basic operation of a computer?

What is the most basic operation of a computer?

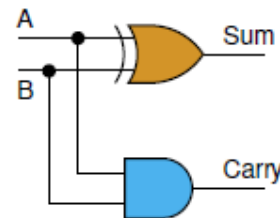
Add two numbers!

- At digital logic level the addition is performed in binary
- Special circuits are used to carry out this operation - **adders**

Half Adders ²²

- **Half adder** – A circuit that computes the sum of two bits and produces the correct carry bit
 - Half adder is fine for adding two single digits, but it **cannot** be used as is to compute the sum of two binary values with multiple digits each

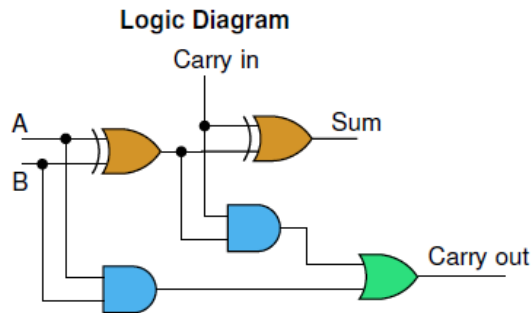
A	B	Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



Full Adders ²³

- A circuit called a **full adder** takes the carry-in value into account.
 - use two half adders to make a full adder

Homework: review how full adder works (Dale. Ch. 4)



Truth Table

A	B	Carry-in	Sum	Carry-out
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

CPU chips

- CPU is an advanced circuit with input and output lines



Recommended reading and videos

1. Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Chapter 4, end of the chapter exercises
2. MIT (2020, June 5). If transistors can't get smaller, then software developers have to get smarter. Tech Xplore - Technology and Engineering news. Retrieved May 31, 2022, from <https://techxplore.com/news/2020-06-transistors-smaller-software-smarter.html>
3. Youtube.com. 2017. Boolean Logic & Logic Gates: Crash Course Computer Science #3. [online] Available at: <<https://www.youtube.com/watch?v=gl-qXk7XojA>> [Accessed 29 May 2022].
4. Youtube.com. 2017. How Computers Calculate - the ALU: Crash Course Computer Science #5 [online] Available at: <<https://www.youtube.com/watch?v=1I5ZMmrOfnA&list=PL8dPuuaLjXtNIUrzyH5r6jN9uIlgZBpdo&index=7>> [Accessed 29 May 2022].

Python

Solutions to previous seminars

Recall countdown function, that prints the numbers from 10 to 0 and prints “Blastoff!”

```
def countdown(n):  
    if n <= 0:  
        print('Blastoff!')  
    else:  
        print(n)  
        countdown(n -1)  
countdown(10)
```

*You were asked on write a countup function. Solution is on the right

```
def countup(n):  
    if n >= 0:  
        print('Blastoff!')  
    else:  
        print(n)  
        countup(n+1)  
countup(-4)
```

Solutions to previous seminars

```
# Code #1 – simple iteration
string_name = "homework"
```

```
# Iterate over the string
for element in string_name:
    print(element, end=' ')
print("\n")
```

```
# Code #2 – range () function
string_name = "HOMEWORK"
```

```
# Iterate over index
for element in range(0, len(string_name)):
    print(string_name[element])
```

Reminder: MyMark (homework from TW3)

Write a program that will ask to input the module name and number of components on the module with corresponding weighting. For example:

Module name: Computer science fundamentals

Number of components: 2

Component 1 weighting: 40%, Component 2 weighting: 60%

Enter mark 1: 70, Enter mark 2: 60

It should also ask to enter mark for the components and show you the final mark.

Additionally you may include a feature, where user can input the desired overall mark for the module and program outputs the required marks for the components.

Save it it in TW4/ folder

Push your updates to Github repository.

Python for beginners in one hour

[Python for Beginners - Learn Python in 1 Hour.](https://www.youtube.com/watch?v=kqtD5dpn9C8)²⁴

²⁴ Hamedani, M., 2020. *Python for Beginners - Learn Python in 1 Hour*. [online] Youtube.com. Available at: <<https://www.youtube.com/watch?v=kqtD5dpn9C8>> [Accessed 5 June 2022].

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