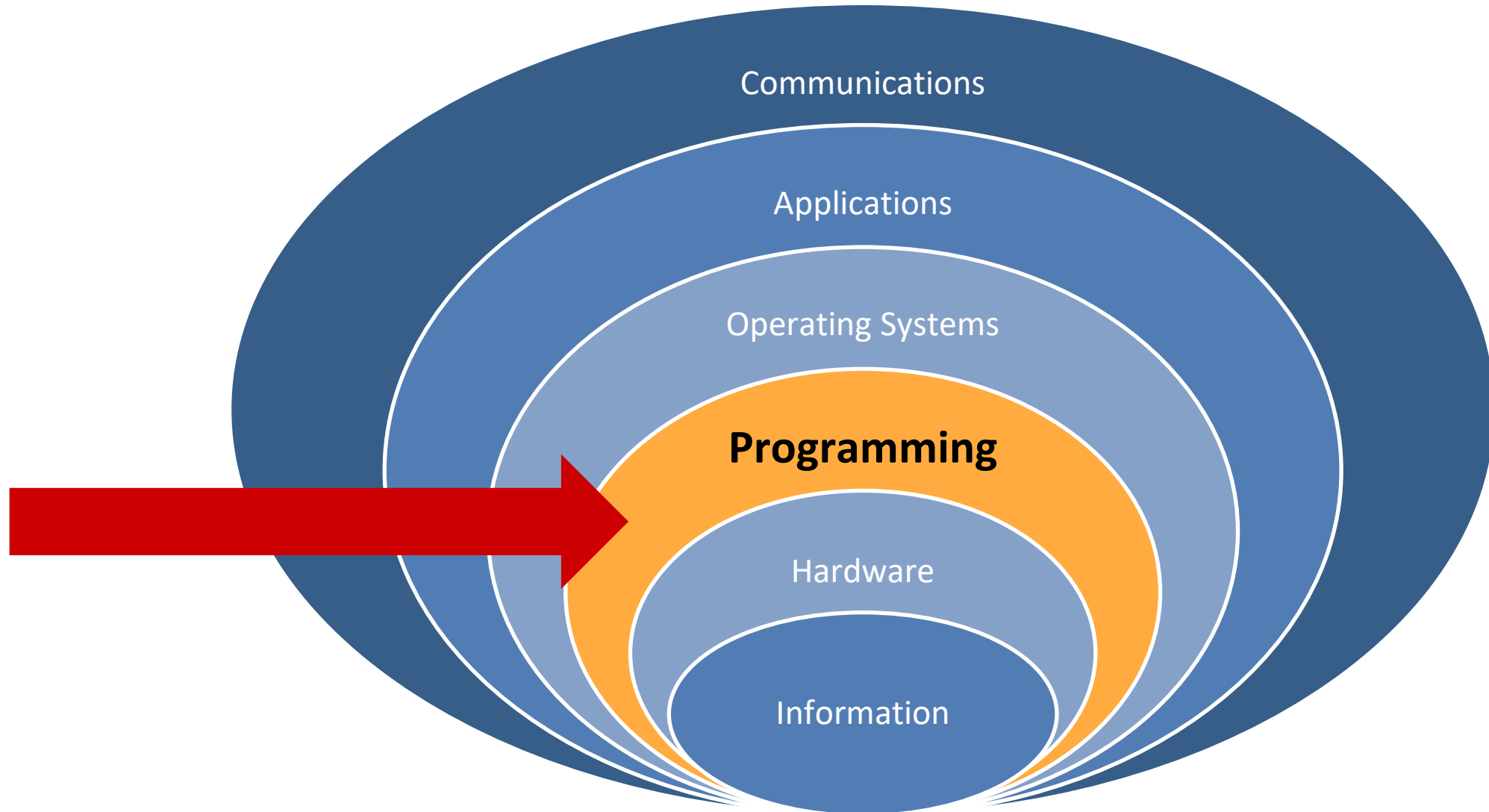


Computer Science Fundamentals

Lecture topic: Programming Layer
Lecturer: Olga Yugay

Today's focus



Agenda

- Problem solving and problem-solving strategies
- Algorithm
- Algorithm with selection
- Algorithm with repetition
- Searching algorithms
 - Sequential search
 - Binary search
- Algorithm complexity

Let's refresh your understanding

[What is Programming? | Intro to JS: Drawing & Animation | Computer programming | Khan Academy](#)¹

¹ Khan Academy. (2015). *What is Programming? | Intro to JS: Drawing & Animation | Computer programming* . Retrieved June 9, 2022, from https://www.youtube.com/watch?v=FCMxA3m_Imc.

Problem solving

- Problem solving - the act of finding a solution to a perplexing question
- A computer is not intelligent
 - Computer can do nothing without being told what to do.
 - Human (the *programmer*) must analyze the problem, develop the instructions for solving the problem (the *program*), and then have the computer carry out the instructions. ²

² Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Problem solving strategies - *heuristics*

- **Ask questions**
 - What do I know about the problem?
 - What is the information that I have to process in order to find the solution?
 - What does the solution look like?
 - What sort of special cases exist?
 - How will I recognize that I have found the solution?
- **Look for Familiar Things**
 - never reinvent the wheel. If a solution exists, use it. If you've solved the same or a similar problem before, just repeat the successful solution.
 - E.g. Use Design Patterns (more about it at level 5)
- **Divide and Conquer**
 - break up a large problem into smaller pieces that we can solve individually.³

³ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

The computer problem-solving process ⁴

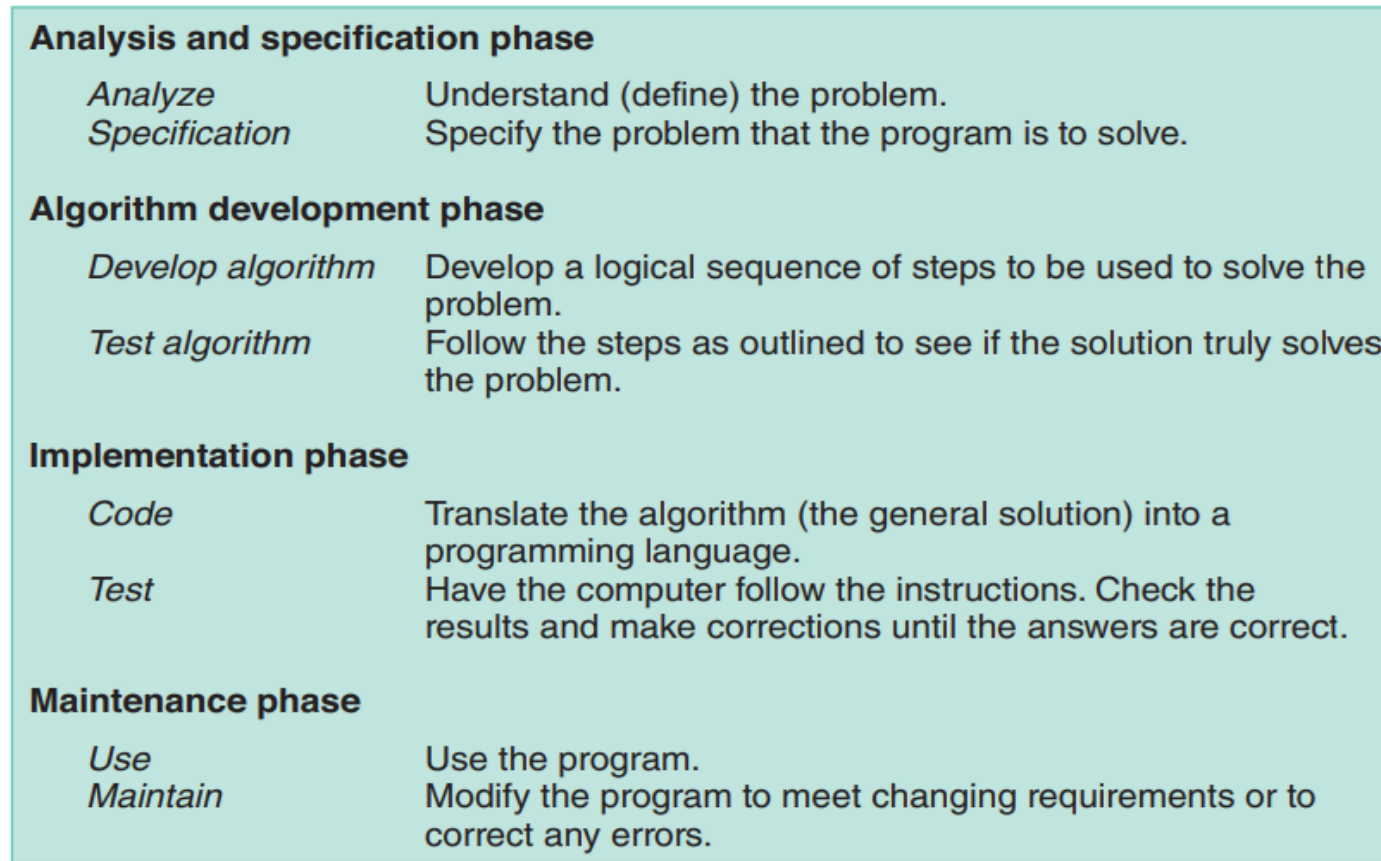


FIGURE 7.2 The computer problem-solving process

⁴ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

The interactions among the problem solving phases

The **black lines** show the general flow through the phase.

The **red lines** represent paths that can be taken to backtrack to a previous phase if a problem occurs. ⁵

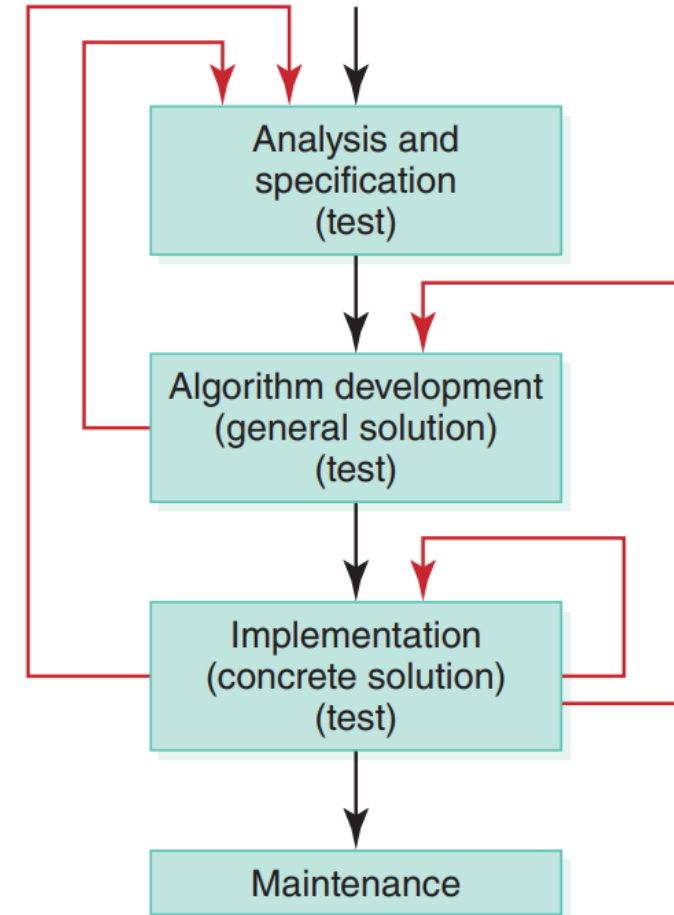


FIGURE 7.3 The interactions among the four problem-solving phases

⁵ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

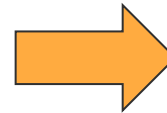
Algorithm

- Algorithm – set of instructions for solving a problem or subproblem in a **finite amount of time** using a **finite amount of data** ⁶
- “Algorithm is a tool for solving a well-specified computational problem. The statement of the problem specifies in general terms the desired input/output relationship. The algorithm describes specific computational procedures for achieving input/output relationship.”
(Cormen et. al.)

⁶ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Presenting algorithm - pseudocode

- *Pseudocode* - uses a mixture of English and formatting to make the steps in the solution explicit. Used to present the algorithm
- Have a look at sample algorithm for **getting up in the morning**⁷



```
Alarm goes off  
Hit sleep button  
Alarm goes off  
Hit sleep button  
Alarm goes off  
Turn off alarm  
Move dog  
Throw back covers  
Put feet over side of the bed  
Stand up
```

⁷ Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

What is algorithm and why you should care?

[What's an algorithm? - David J. Malan](#) ⁸

[What is algorithm and why should you care?](#) ⁹

⁸ Malan, D. J. (2013, May 20). What's an algorithm? - David J. Malan. YouTube. Retrieved June 9, 2022, from <https://youtu.be/6hfOvs8pY1k>

⁹ Khan Academy. (2015, July 27). What is an algorithm and why should you care? | algorithms | computer science . YouTube. Retrieved June 9, 2022, from <https://www.youtube.com/watch?v=CvSOaYi89B4>

Summary of methodology for designing algorithms¹⁰

1. Analyze the Problem
 - a. list information to work with (data)
 - b. specify potential solution
 - c. list assumptions
 - d. develop overall plan
2. List the Main Tasks
 - a. Main module
3. Write the Remaining Modules
 - a. modules on one level can specify more modules on lower levels
4. Re-sequence and Revise as Necessary

¹⁰Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Algorithms with selection¹¹

Case: write an algorithm to express what dress is appropriate for a given outside temperature.

Write "Enter the temperature"

Read temperature

Determine dress

Determine dress

IF (temperature > 90)

Write "Texas weather: wear shorts"

ELSE IF (temperature > 70)

Write "Ideal weather: short sleeves are fine"

ELSE IF (temperature > 50)

Write "A little chilly: wear a light jacket"

ELSE IF (temperature > 32)

Write "Philadelphia weather: wear a heavy coat"

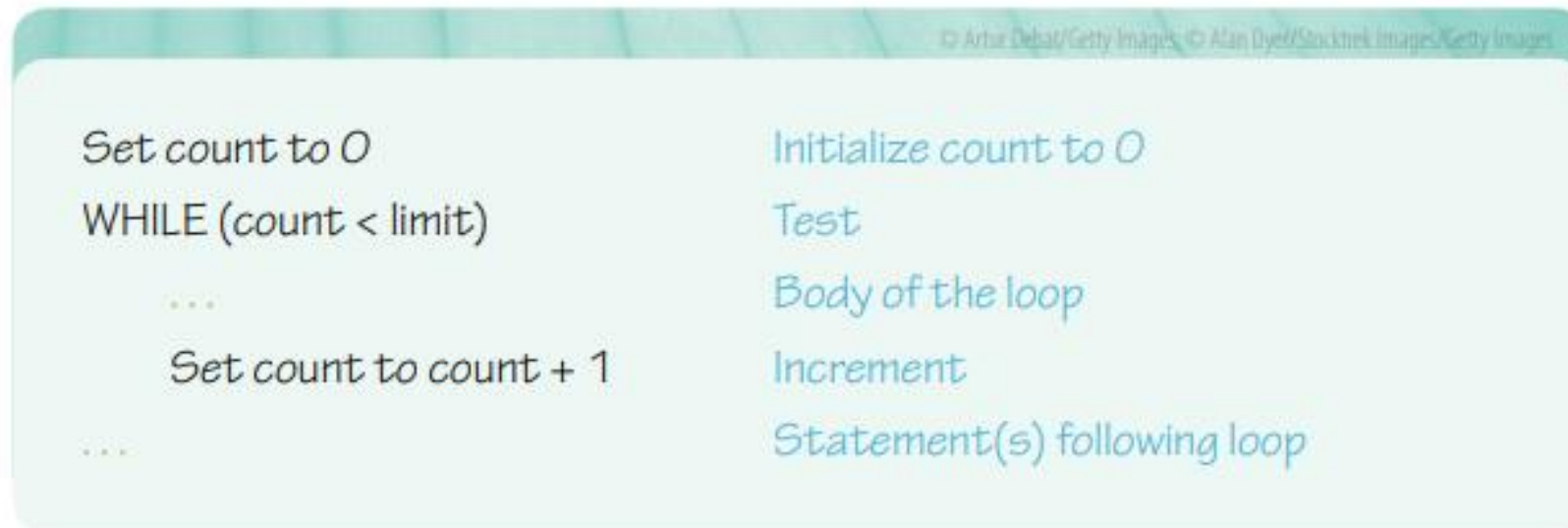
ELSE

Write "Stay inside"

¹¹Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Algorithms with repetition ¹²

Count-controlled loops



¹²Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Algorithms with repetition ¹³

Event-controlled loops

When implementing an event-controlled loop using a while statement, there are again three parts to the process:

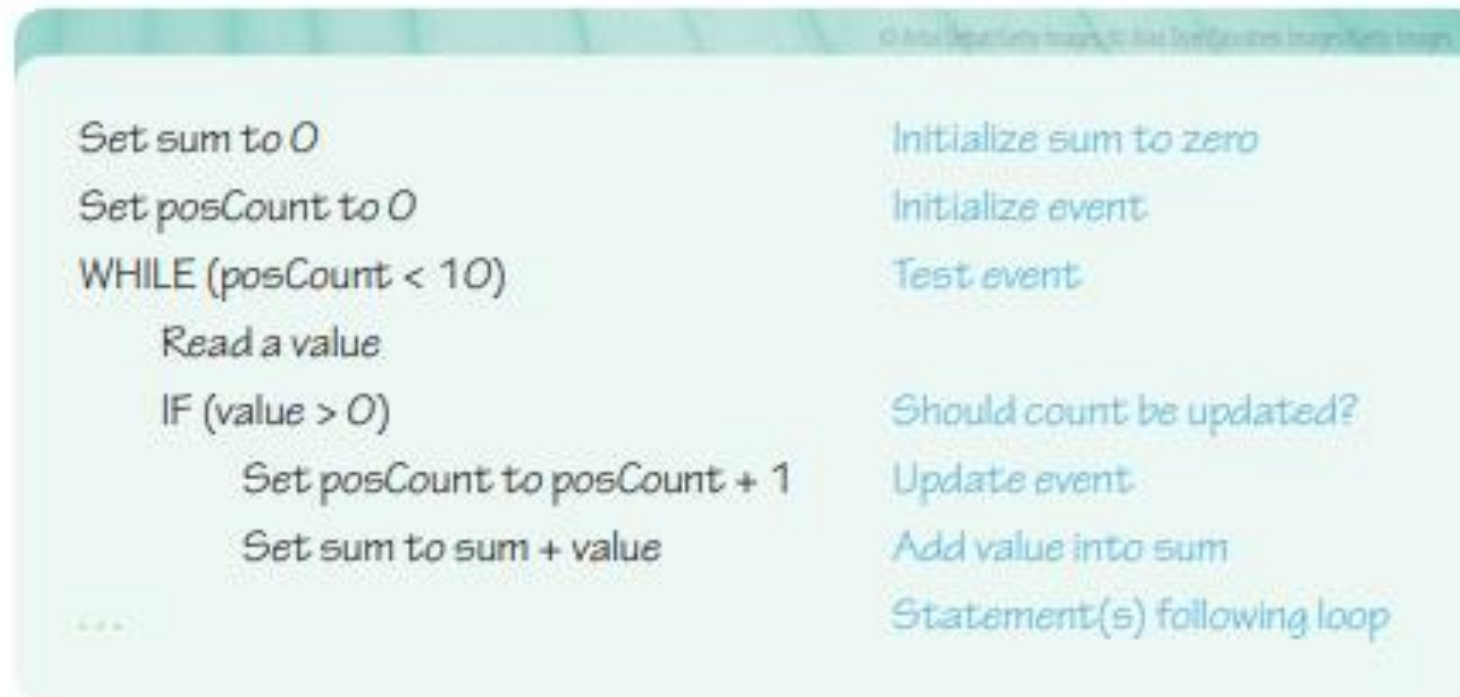
1. the event must be initialized
2. the event must be tested
3. and the event must be updated



The algorithm on the right reads and sums data values until a negative value is read

Algorithms with repetition ¹⁴

event controlled loop continued



Searching algorithms: sequential search ¹⁵

Each item is looked at in turn and compared to the one being searched.

Stop either when the item is found, or when all items are looked at and not found a match

```
Set position to 0
Set found to FALSE
WHILE (position < 10 AND found is FALSE)
  IF (numbers[position] equals searchItem)
    Set found to TRUE
  ELSE
    Set position to position + 1
```

Searching algorithm: Binary search ¹⁶

Binary search is an efficient algorithm for finding an item from a sorted list of items. It works by repeatedly dividing in half the portion of the list that could contain the item, until you've narrowed down the possible locations to just one.

Watch video on [binary search algorithm](#) ¹⁷

¹⁶Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

¹⁷HackerRank. (2016, September 27). Algorithms: Binary search. YouTube. Retrieved June 9, 2022, from <https://www.youtube.com/watch?v=P3YID7liBug>

Example

Given list of numbers find number 5

1, 2, 5, 7, 8, 10, 50, 60, 71, 77, 78, 79, 80

$x=5$

Example

Given list of numbers find number 5

1, 2, 5, 7, 8, 10, 50, 60, 71, 77, 78, 79, 80

$x=5$



1) Midpoint is 50 ($13/2=6.5$, 7th number is the midpoint)

To identify midpoint:

1. Count the total number of number entries (which is 13 in this example)
2. Divide the total number by 2 (in this example, $13/2=6.5$)
3. Round the result $6.5 \approx 7$, 7th number is the midpoint

Example

Given list of numbers find number 5

1, 2, 5, 7, 8, 10, ~~50, 60, 71, 77, 78, 79, 80~~

$x=5$

- 1) Midpoint is 50 ($13/2=6.5$, 7th number is the midpoint)
- 2) $x < \text{midpoint}$ ($5 < 50$), ignore the range on the right (50-80)

Example

Given list of numbers find number 5

1, 2, 5, 7, 8, 10, ~~50, 60, 71, 77, 78, 79, 80~~

x=5



- 1) Midpoint is 50 ($13/2=6.5$, 7th number is the midpoint)
- 2) $x < \text{midpoint}$ ($5 < 50$), ignore the range on the right (50-80)
- 3) Midpoint is 5

To identify new midpoint:

1. Count the total number of left number entries (which is 6)
2. Divide the total number by 2 (in this example, $6/2=3$,
3. 3rd number is the new midpoint

Example

Given list of numbers find number 5

1, 2, 5, 7, 8, 10, ~~50, 60, 71, 77, 78, 79, 80~~

$x=5$

- 1) Midpoint is 50 ($13/2=6.5$, 7th number is the midpoint)
- 2) $x < \text{midpoint}$ ($5 < 50$), ignore the range on the right (50-80)
- 3) Midpoint is 5
- 4) x is equal to midpoint ($5==5$). The number is found!

Algorithm complexity¹⁸

Complexity estimates how an algorithm performs regardless the kind of machine it runs on.

- **time complexity** - the amount of time algorithm needs to execute and produce the result
- **space complexity** - the amount of memory used by the algorithm (including the input values to the algorithm) to execute and produce the result.

¹⁸Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9

Algorithm complexity

Complexity is defined as function of the input size n using Big-O notation.

n indicates the size of the input

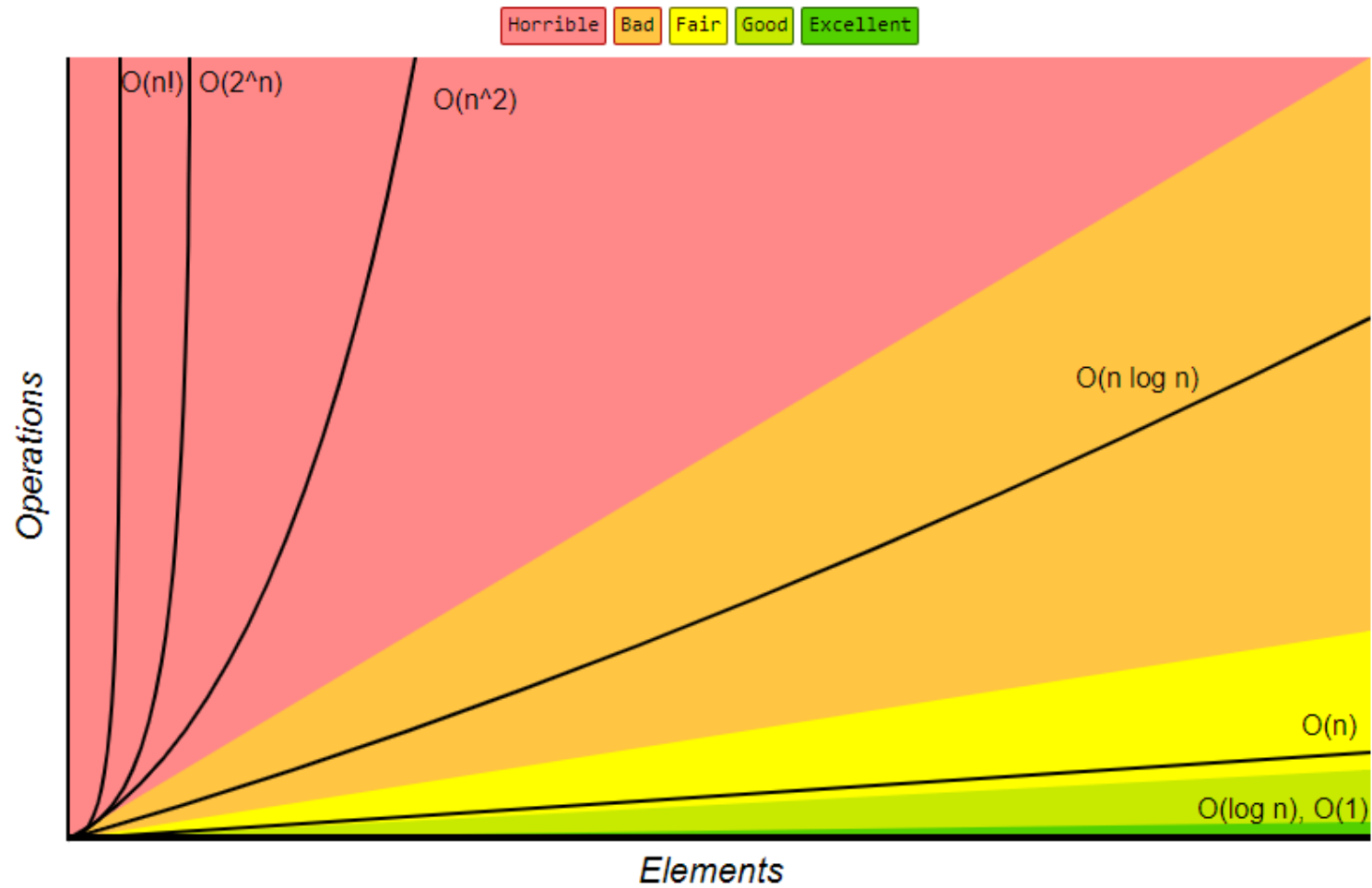
O is the worst-case scenario growth rate function.

- $O(1)$ - the algorithm takes the same amount of time to compute regardless of the input size.
- $O(n)$ - linear time, as the input grows, the algorithms take proportionally longer to complete
- $O(\log n)$ - logarithmic time complexity, a time execution is proportional to the logarithm of the input size

And others... Have a look here: [8 time complexities that every programmer should know](#)¹⁹

¹⁹Mejia, A. (2019, September 19). *8 time complexities that every programmer should know*. Adrian Mejia Blog. Retrieved June 9, 2022, from <https://adrianmejia.com/most-popular-algorithms-time-complexity-every-programmer-should-know-free-online-tutorial-course/>

Algorithm complexity



Common data structure operations

Common Data Structure Operations

Data Structure	Time Complexity								Space Complexity
	Average				Worst				Worst
	Access	Search	Insertion	Deletion	Access	Search	Insertion	Deletion	
<u>Array</u>	$\theta(1)$	$\theta(n)$	$\theta(n)$	$\theta(n)$	$\theta(1)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<u>Stack</u>	$\theta(n)$	$\theta(n)$	$\theta(1)$	$\theta(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<u>Queue</u>	$\theta(n)$	$\theta(n)$	$\theta(1)$	$\theta(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<u>Singly-Linked List</u>	$\theta(n)$	$\theta(n)$	$\theta(1)$	$\theta(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<u>Doubly-Linked List</u>	$\theta(n)$	$\theta(n)$	$\theta(1)$	$\theta(1)$	$O(n)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
<u>Skip List</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n \log(n))$
<u>Hash Table</u>	N/A	$\theta(1)$	$\theta(1)$	$\theta(1)$	N/A	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<u>Binary Search Tree</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<u>Cartesian Tree</u>	N/A	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	N/A	$O(n)$	$O(n)$	$O(n)$	$O(n)$
<u>B-Tree</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<u>Red-Black Tree</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<u>Splay Tree</u>	N/A	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	N/A	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<u>AVL Tree</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$
<u>KD Tree</u>	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$\theta(\log(n))$	$O(n)$	$O(n)$	$O(n)$	$O(n)$	$O(n)$

²¹Know thy complexities! Big. (n.d.). Retrieved June 9, 2022, from <https://www.bigocheatsheet.com/>

Array sorting algorithms

Algorithm	Time Complexity			Space Complexity
	Best	Average	Worst	Worst
<u>Quicksort</u>	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n^2)$	$O(\log(n))$
<u>Mergesort</u>	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(n)$
<u>Timsort</u>	$\Omega(n)$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(n)$
<u>Heapsort</u>	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(1)$
<u>Bubble Sort</u>	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
<u>Insertion Sort</u>	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
<u>Selection Sort</u>	$\Omega(n^2)$	$\Theta(n^2)$	$O(n^2)$	$O(1)$
<u>Tree Sort</u>	$\Omega(n \log(n))$	$\Theta(n \log(n))$	$O(n^2)$	$O(n)$
<u>Shell Sort</u>	$\Omega(n \log(n))$	$\Theta(n(\log(n))^2)$	$O(n(\log(n))^2)$	$O(1)$
<u>Bucket Sort</u>	$\Omega(n+k)$	$\Theta(n+k)$	$O(n^2)$	$O(n)$
<u>Radix Sort</u>	$\Omega(nk)$	$\Theta(nk)$	$O(nk)$	$O(n+k)$
<u>Counting Sort</u>	$\Omega(n+k)$	$\Theta(n+k)$	$O(n+k)$	$O(k)$
<u>Cubesort</u>	$\Omega(n)$	$\Theta(n \log(n))$	$O(n \log(n))$	$O(n)$

Recommended sources:

- [Computer Science Illuminated, Chapter 7-9, end of the book exercises](#)
- [What is algorithm and why should you care? \[video\]](#)
- <https://adrianmejia.com/most-popular-algorithms-time-complexity-every-programmer-should-know-free-online-tutorial-course/>
- Explore:
 - <http://carlcheo.com/startcoding>
 - <http://carlcheo.com/wp-content/uploads/2014/12/which-programming-language-should-i-learn-first-infographic.png>

References

1. Dale, N., & Lewis, J. (2020). Computer Science Illuminated (7th ed.). Jones & Bartlett Learning, Ch 7-9
2. Khan Academy. (2015). What is Programming? | Intro to JS: Drawing & Animation | Computer programming . Retrieved June 9, 2022, from https://www.youtube.com/watch?v=FCMxA3m_Imc.
3. Malan, D. J. (2013, May 20). *What's an algorithm? - David J. Malan*. YouTube. Retrieved June 9, 2022, from <https://youtu.be/6hfOvs8pY1k>
4. HackerRank. (2016, September 27). *Algorithms: Binary search*. YouTube. Retrieved June 9, 2022, from <https://www.youtube.com/watch?v=P3YID7liBug>
5. Mejia, A. (2019, September 19). *8 time complexities that every programmer should know*. Adrian Mejia Blog. Retrieved June 9, 2022, from <https://adrianmejia.com/most-popular-algorithms-time-complexity-every-programmer-should-know-free-online-tutorial-course/>
6. *Know thy complexities!* Big. (n.d.). Retrieved June 9, 2022, from <https://www.bigocheatsheet.com/>
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Thank you